

Experiment and ImQMD comparison using Flow parameters of Xe + Sn @ 100 AMeV and Ni + Ni @ 52 AMeV

2025 CENuM Workshop in Jeju



**2025.1.16.木
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Physics Motivation

Nuclear symmetry energy

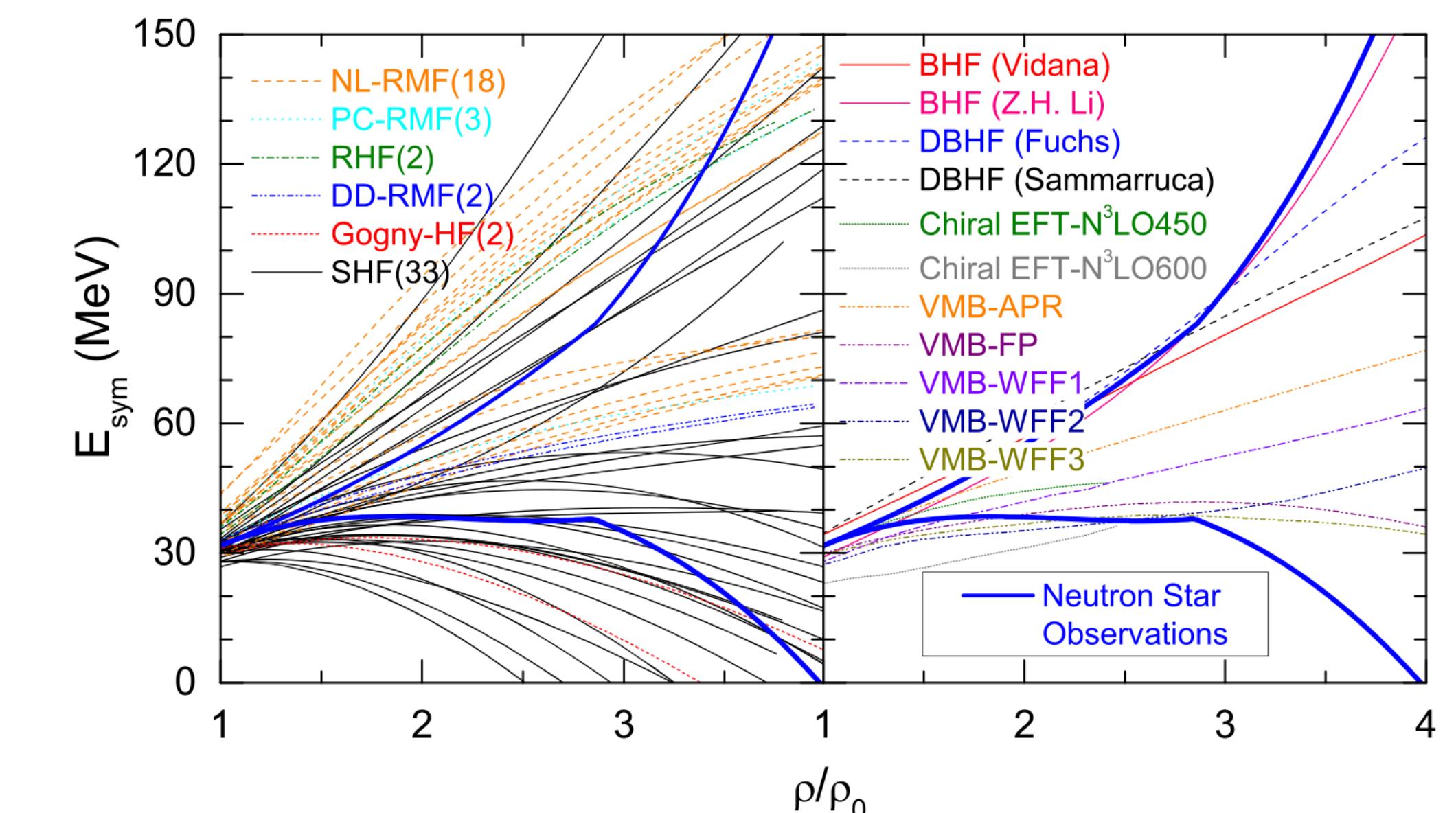
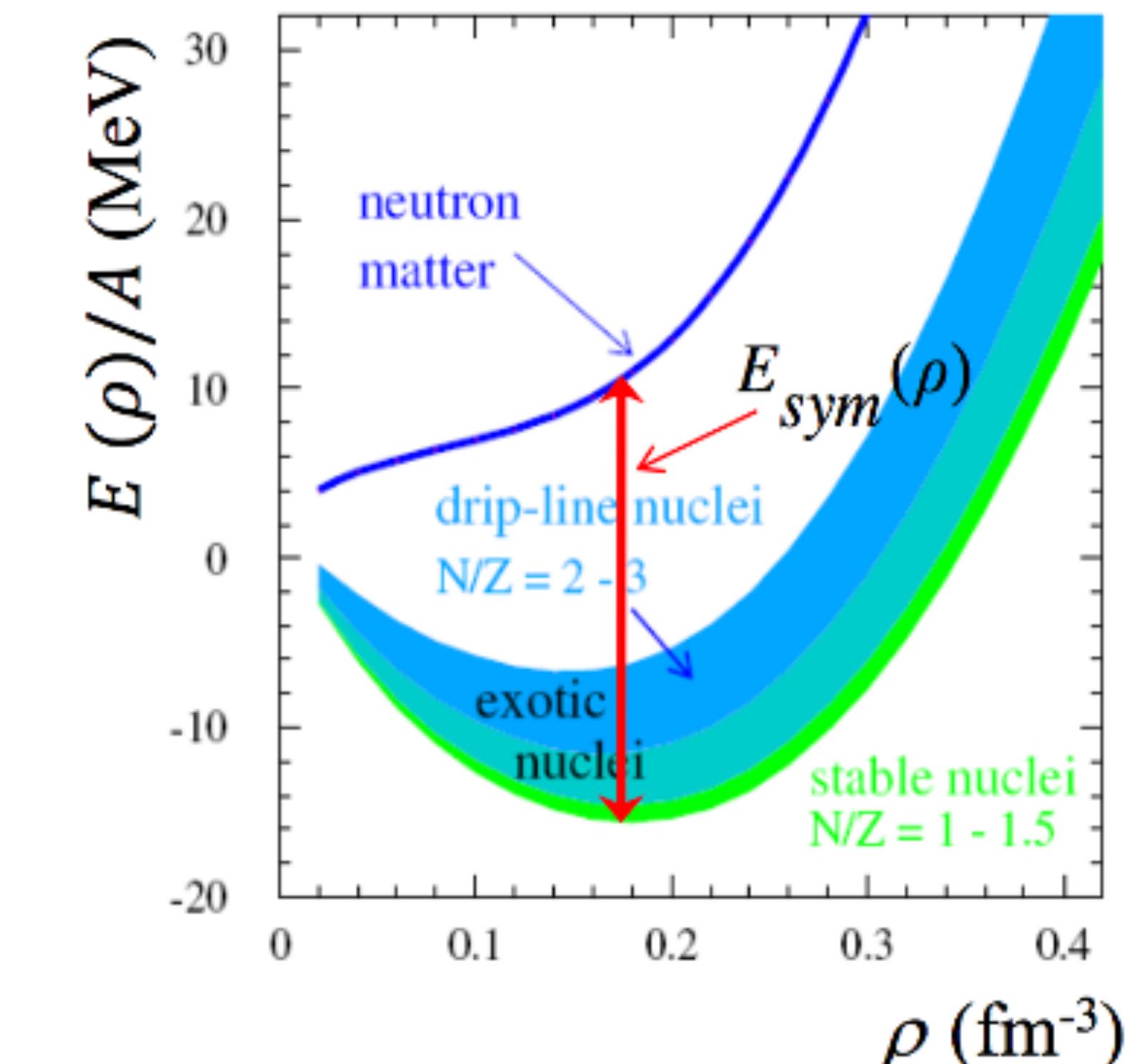
$$E(\rho, \delta)/A = E(\rho_n = \rho_p) + E_{sym}(\rho)\delta^2$$

Iso scalar Iso vector

$$E_{sym}(\rho) = \frac{1}{2} \frac{\partial^2 E}{\partial \delta^2} \sim E(\rho_{\text{pure neutron}}) - E(\rho_{\text{symmetric}})$$

$$\rho = \rho_n + \rho_p, \quad \delta = (\rho_n - \rho_p)/\rho$$

$$E_{sym}(\rho) = S + \frac{L_{sym}}{3} \left(\frac{\rho - \rho_0}{\rho_0} \right) + \frac{K_{sym}}{18} \left(\frac{\rho - \rho_0}{\rho_0} \right)^2$$



Collective flow

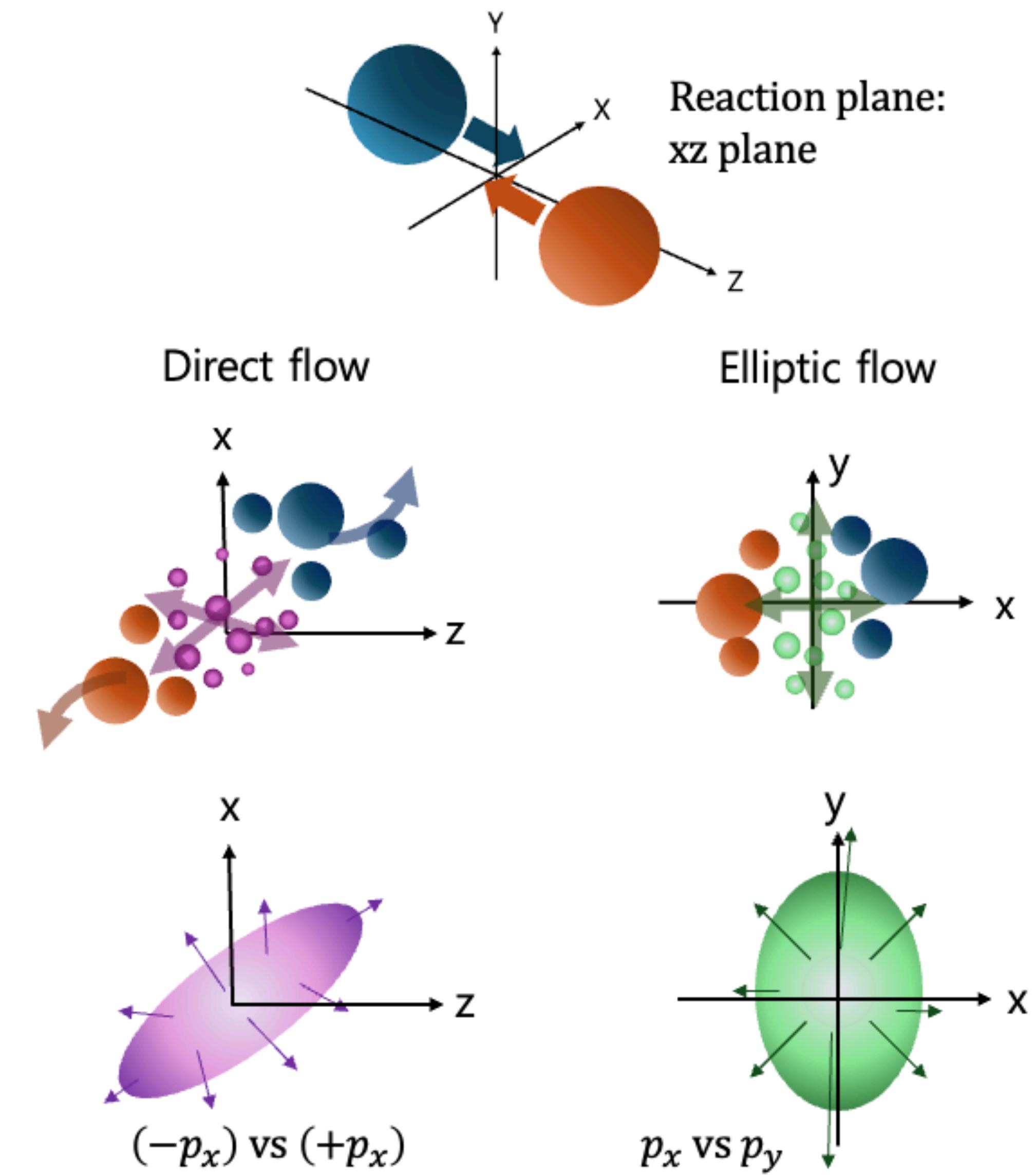
Fourier expansion of azimuthal distribution

$$\frac{dN}{d(\phi - \psi_r)} = \frac{N_0}{2\pi} \left(1 + \sum_{n \geq 1} 2v_n \cos(\phi - \psi_{rp}) \right)$$

v_1 : Direct flow , v_2 : Elliptic flow

$$v_1 = \langle \cos(\phi - \psi_r) \rangle = \left\langle \frac{p_x}{p_t} \right\rangle$$

$$v_2 = \langle \cos 2(\phi - \psi_r) \rangle = \left\langle \frac{p_x^2 - p_y^2}{p_t^2} \right\rangle$$



Data sets

Experiment and ImQMD with 2 parameter sets

INDRA 4th campaign at GSI (1998-1999)
(INDRA-ALADIN collaboration)



E789 at GANIL (2019.4->5)
(INDRA-FAZIA collaboration)



$^{129,124}\text{Xe} + ^{124,112}\text{Sn}$
@ 100MeV/u

$^{64,58}\text{Ni} + ^{64,58}\text{Ni}$
@ 52MeV/u

ImQMD with 2 Skyrme parameters

Para	ρ_0	E_0	K_0	S_0	L
SLy4	0.160	-15.97	230	32	46
SkM*	0.160	-15.77	217	30	46
	K_{sym}	m^*/m	m_n^*/m	m_p^*/m	
SLy4	-120	0.69	0.68	0.71	
SkM*	-156	0.79	0.82	0.76	

Impact parameter windows

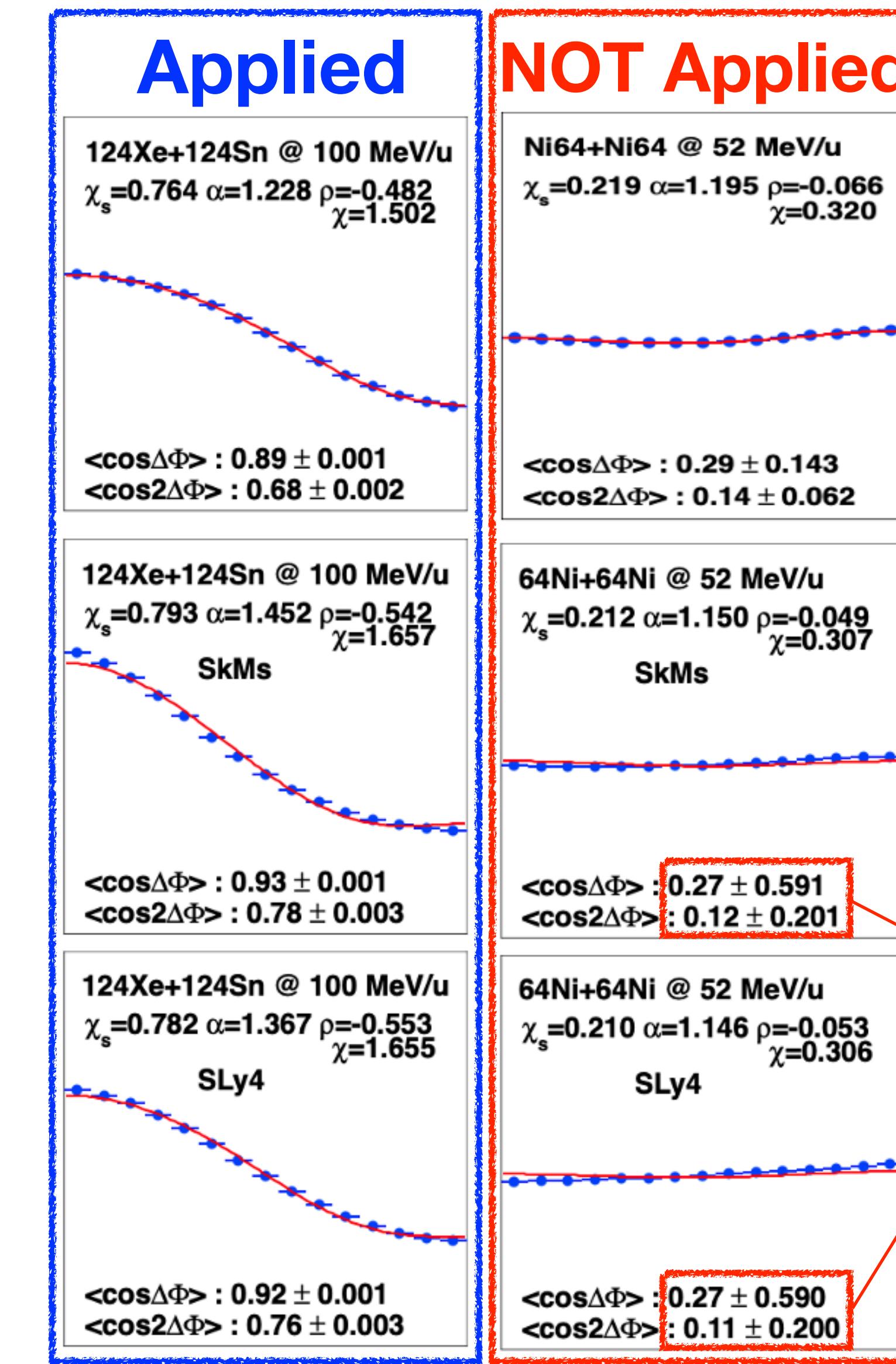
INDRA Camp 4th	IW1 ($0.21 < b_0 < 0.42$)
E789	EW1 ($0.03 < b_0 < 0.4$)

Reaction plane reconstruction and correction factor

Transverse momentum method

$$Q = \sum_{i \neq poi}^N \omega_i (\mathbf{p}_t^i + m_i \mathbf{v}_b)$$

$$\mathbf{v}_b = \frac{\mathbf{p}_t}{m_{sys} - m_{poi}} \quad \begin{aligned} \omega_i &= Z_i (y_{cm} > 0) \\ &= -Z_i (y_{cm} < 0) \end{aligned}$$

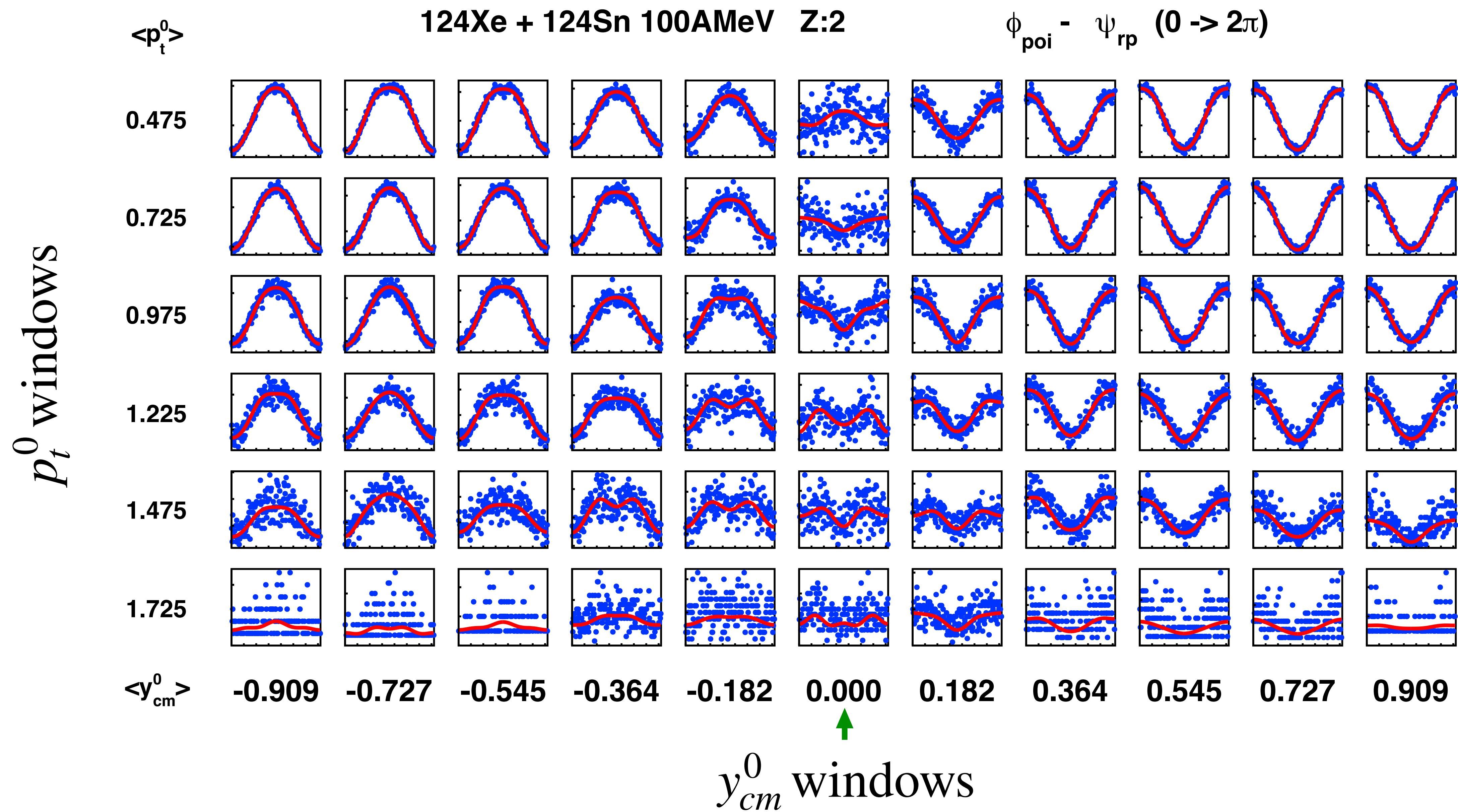


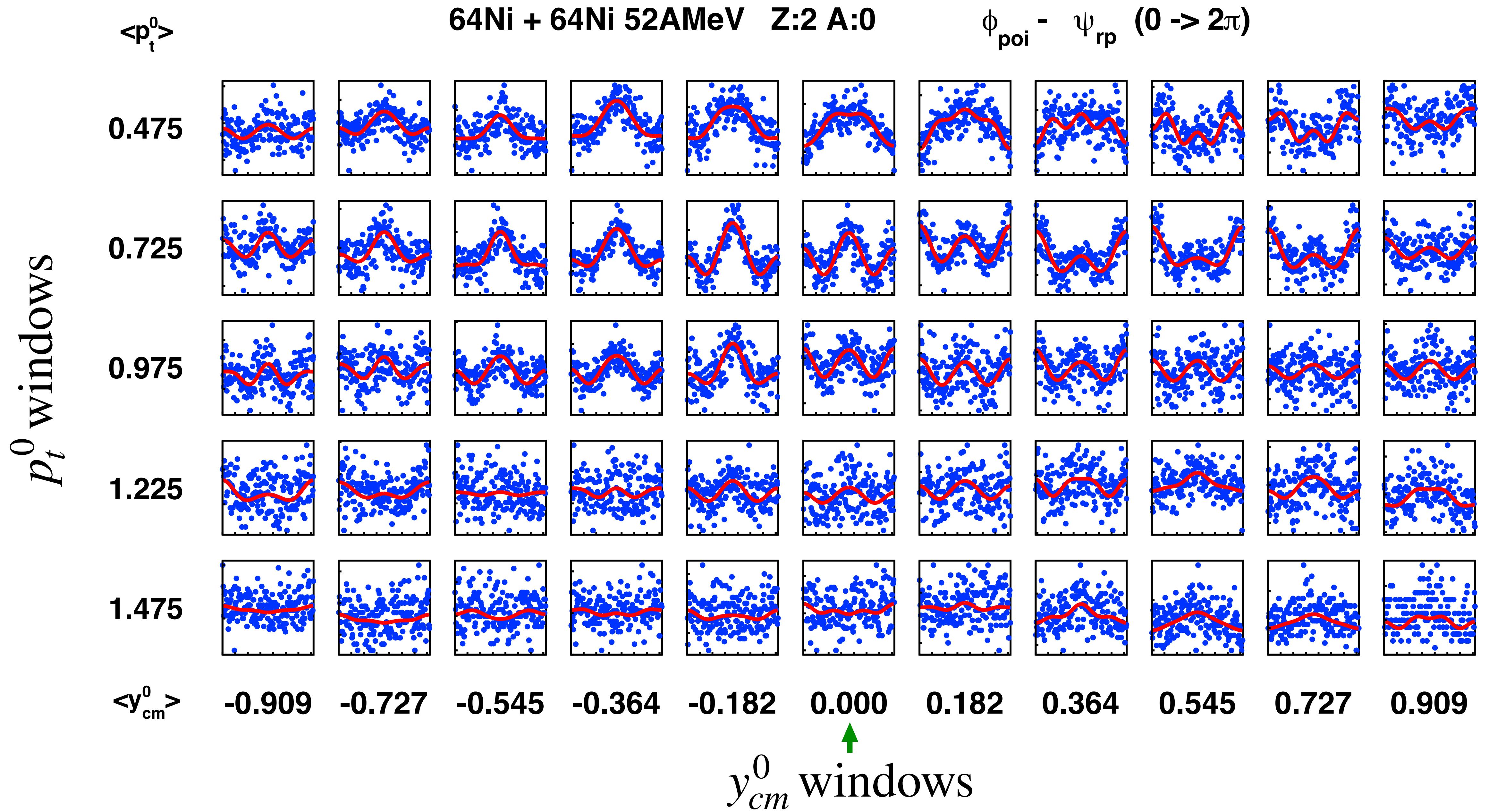
$0 \rightarrow \pi$ [rad]

Too large
Error!

$$\text{Fit: } y = \frac{N_0}{2\pi} \left(1 + 2 \sum_{n=1}^4 v_n \cos(\phi_{poi} - \psi_{rp}) \right)$$

v_1 : Direct, v_2 : Elliptic, v_3 : triangular ...





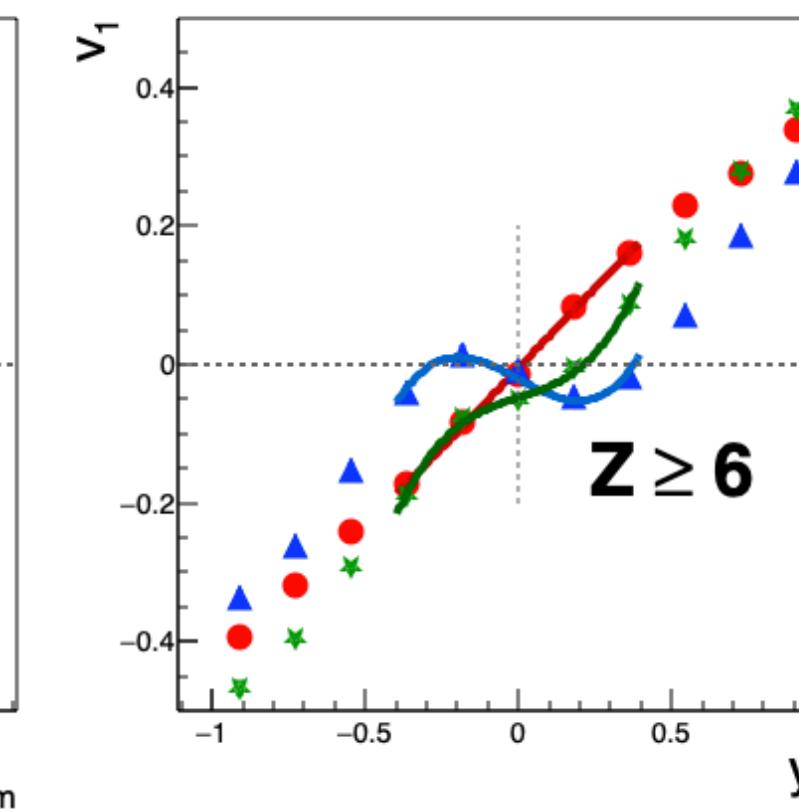
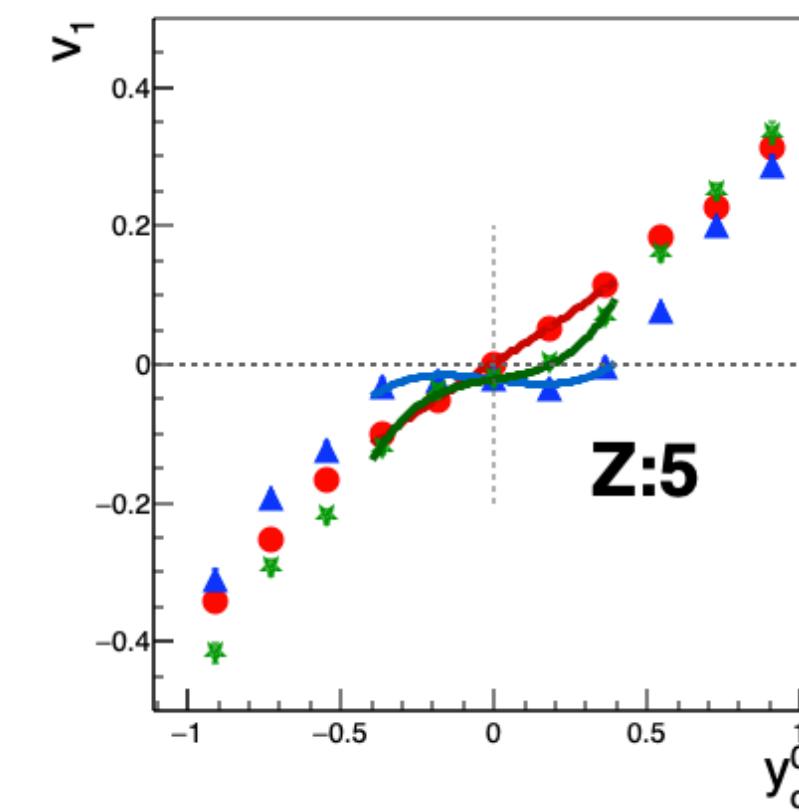
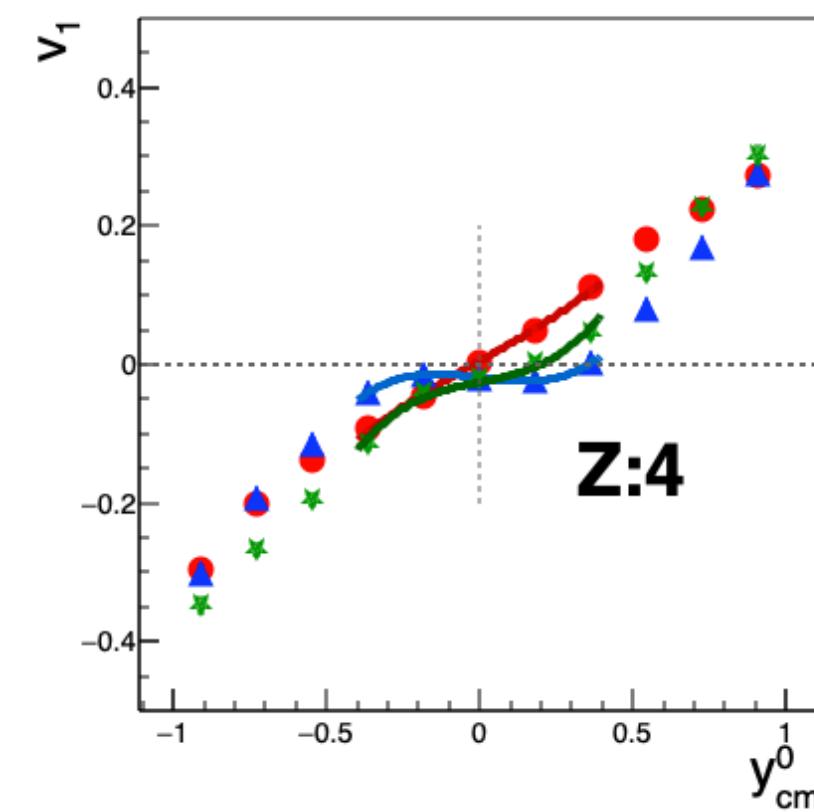
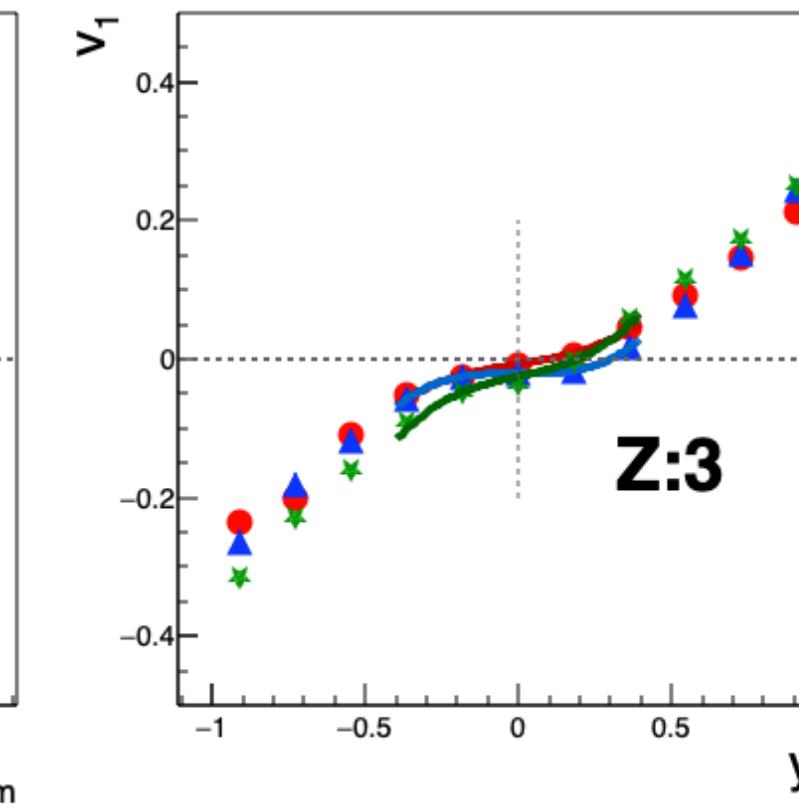
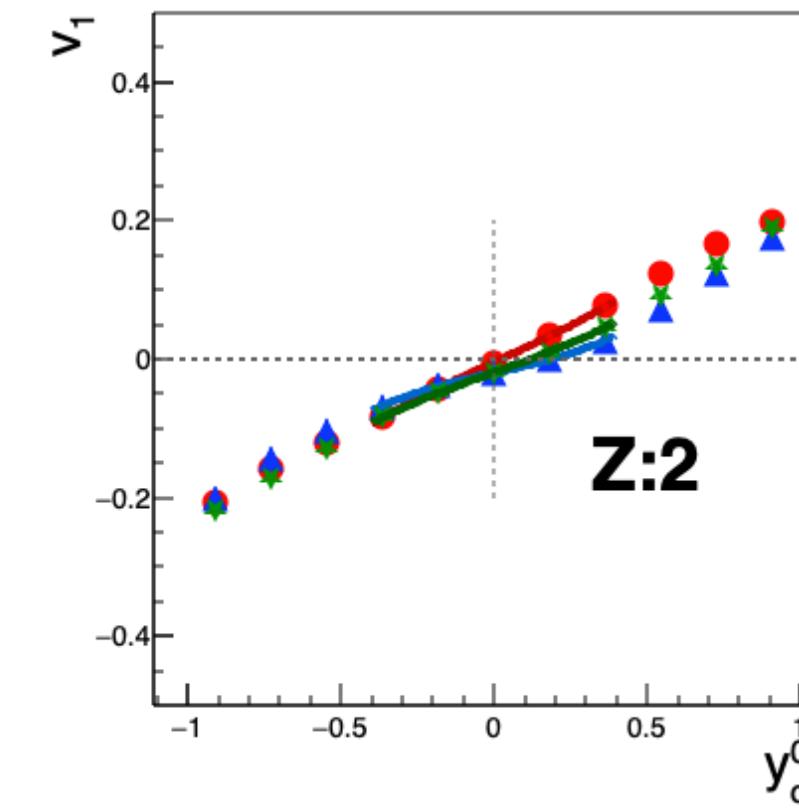
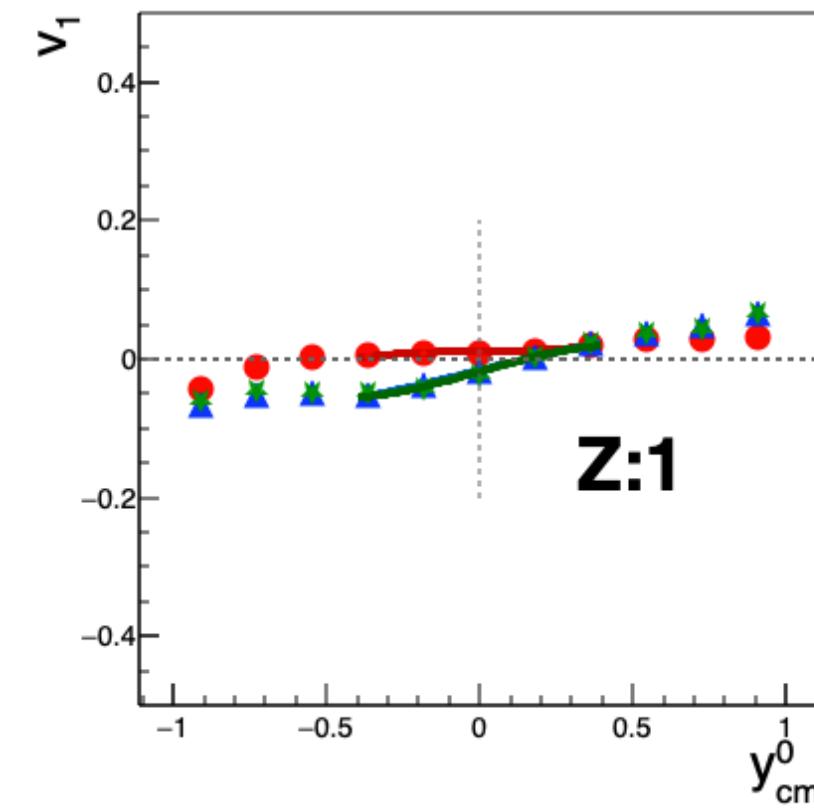
Direct flow vs y_{cm}^0

IW1, Fit : $y = ax^3 + bx + c$, $0.35 < p_t^0 < 0.60$

Exp

SLy4

SkMs



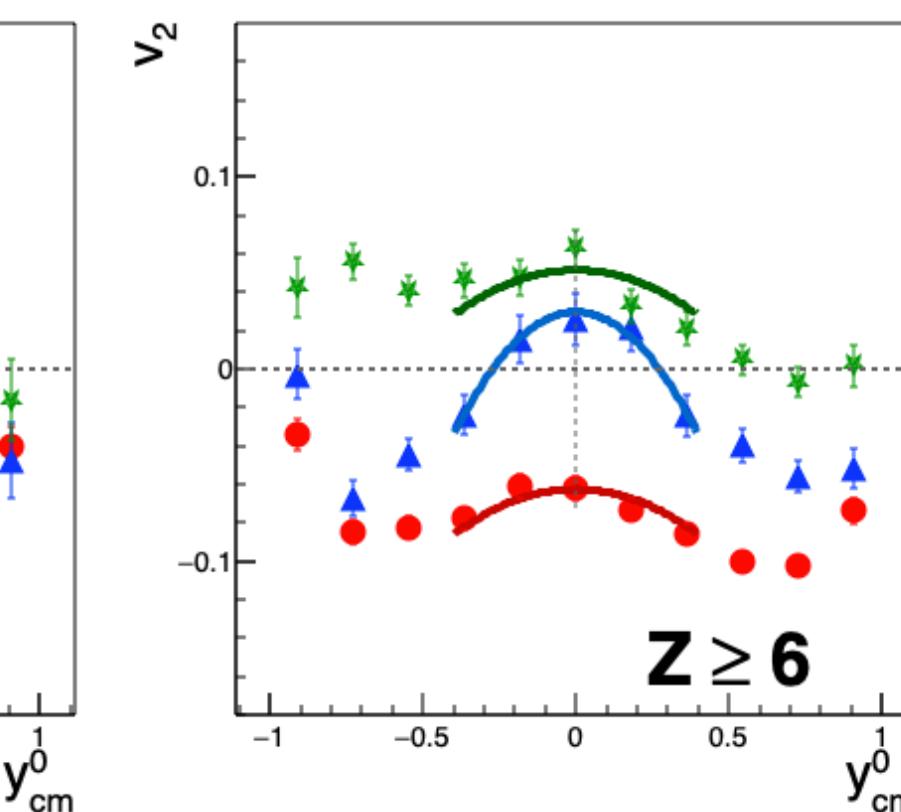
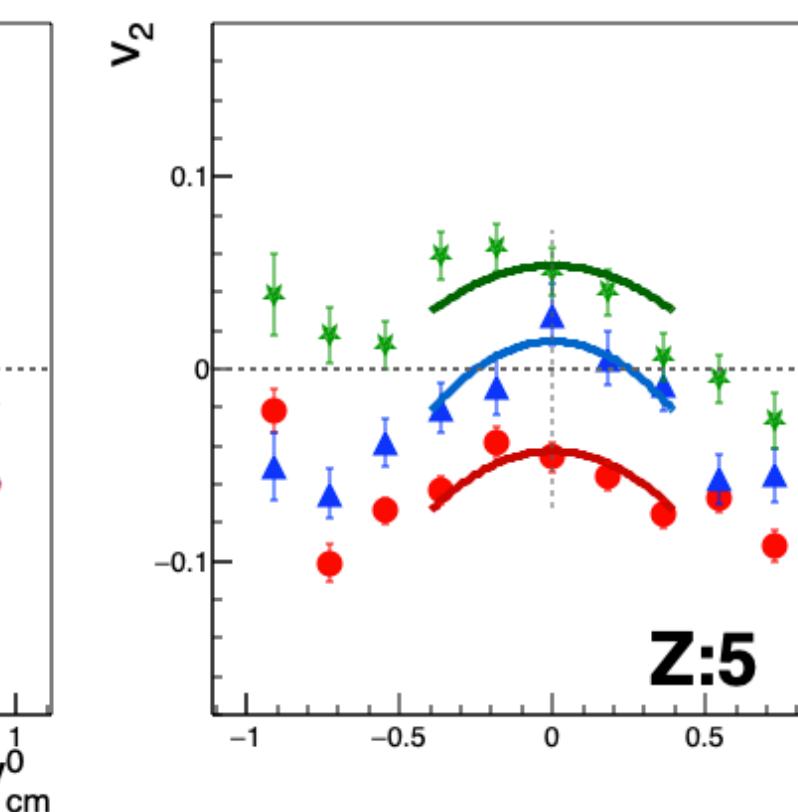
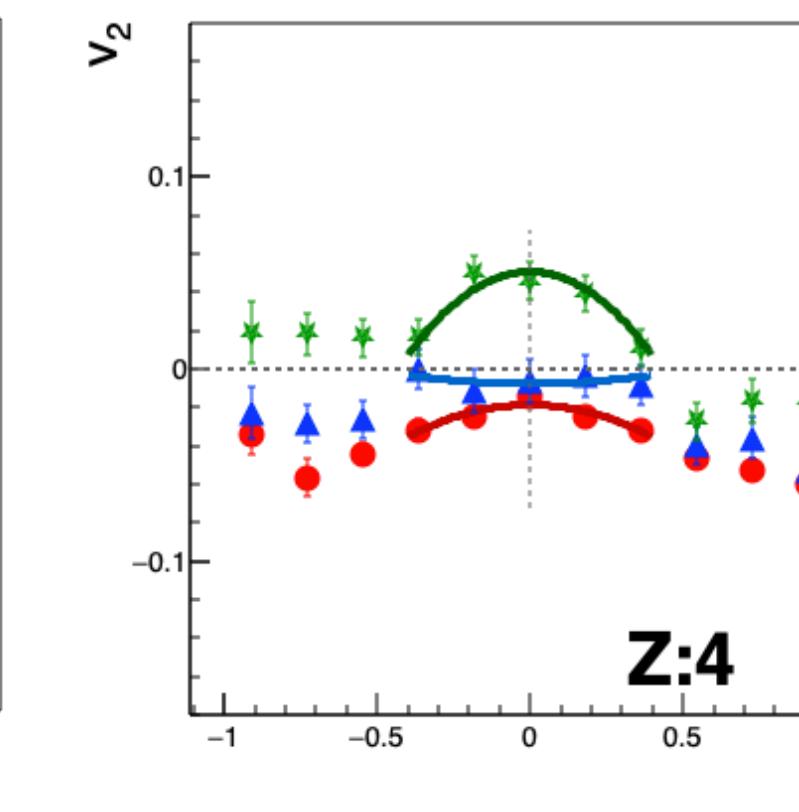
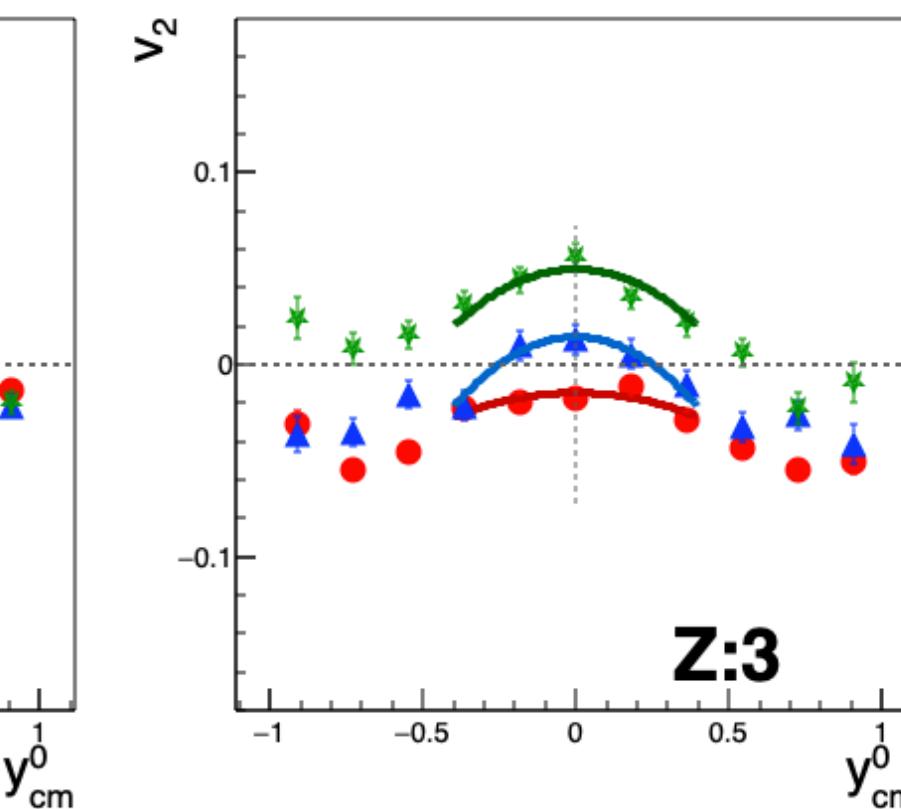
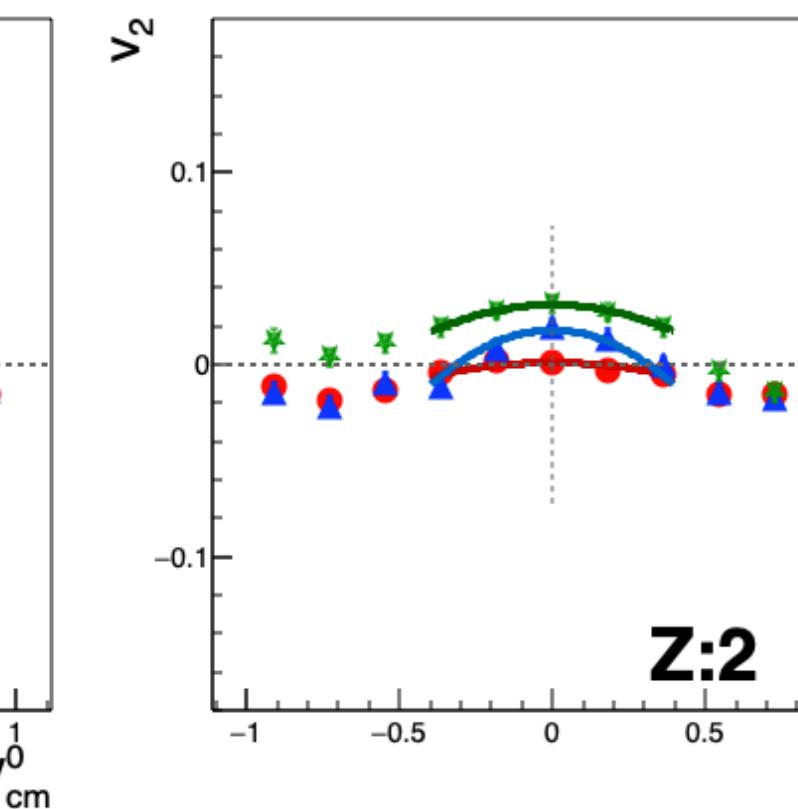
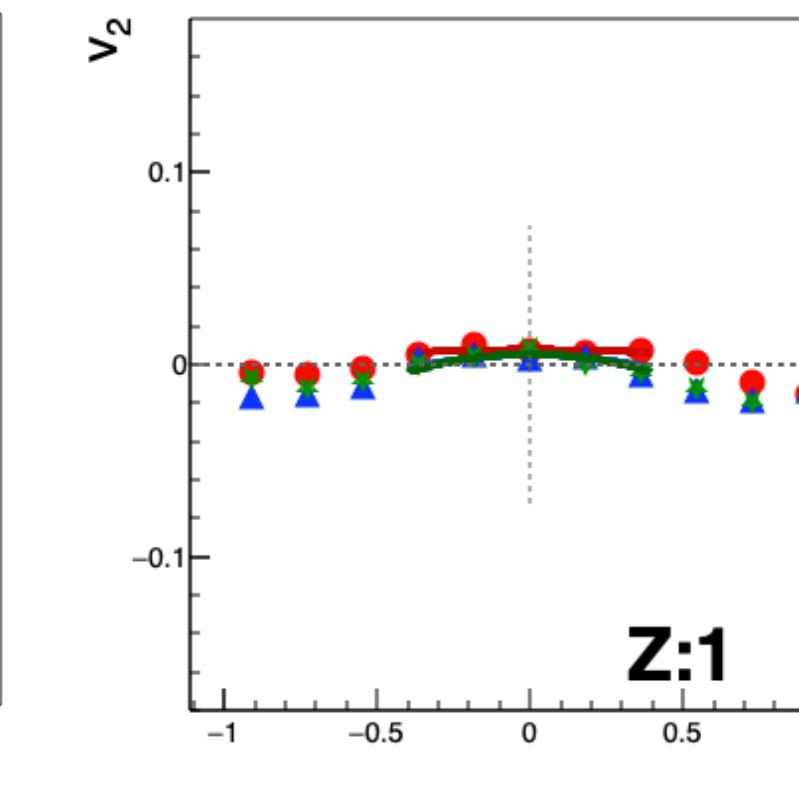
Elliptic flow vs y_{cm}^0

IW1, Fit : $y = ax^2 + b$, $0.35 < p_t^0 < 0.60$

Exp

SLy4

SkMs



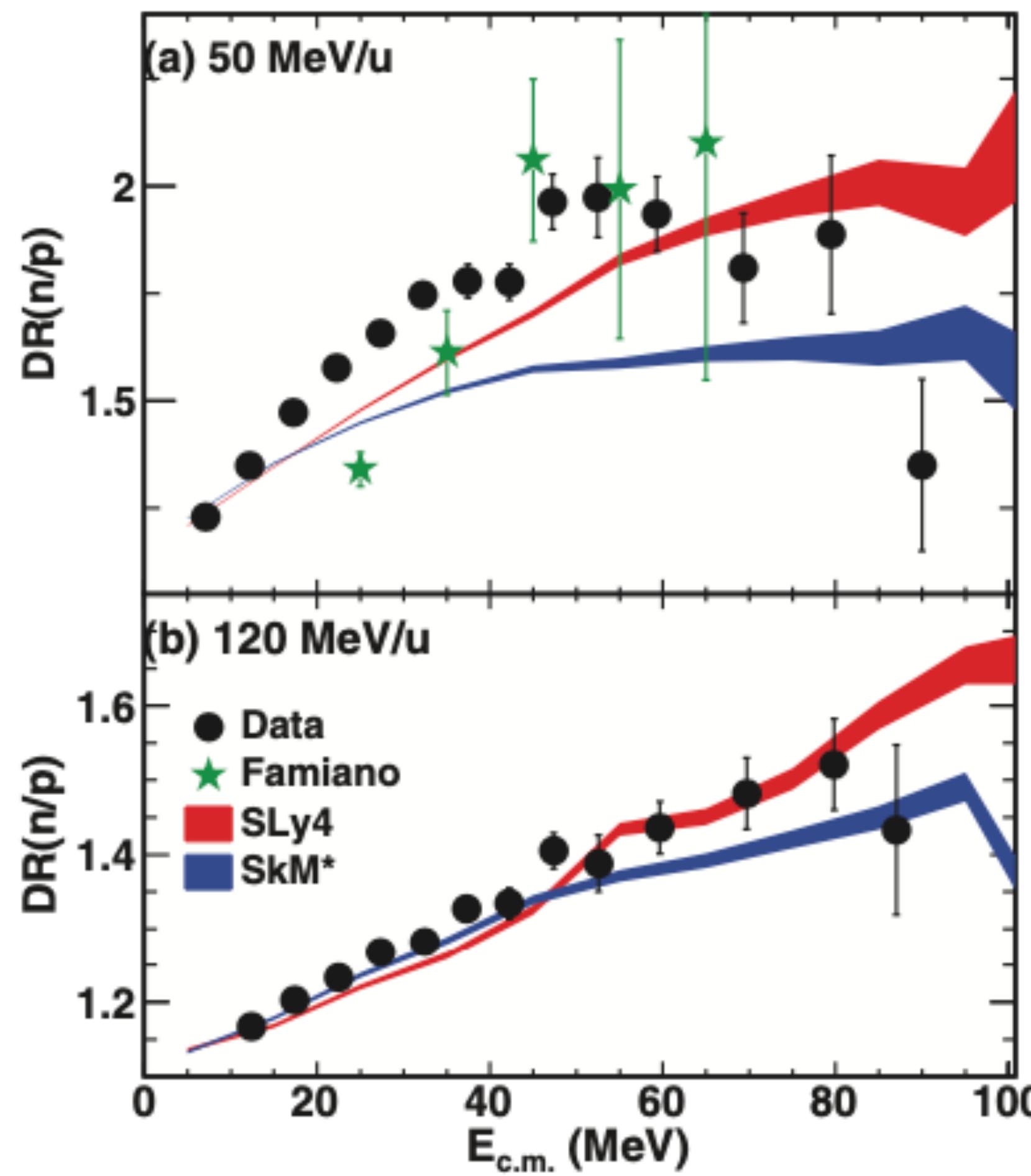
Parameter b : Slope of Direct flow

$$y_{cm}^0 = y_{cm}/y_{cm}^P \quad (y_{cm} > 0)$$

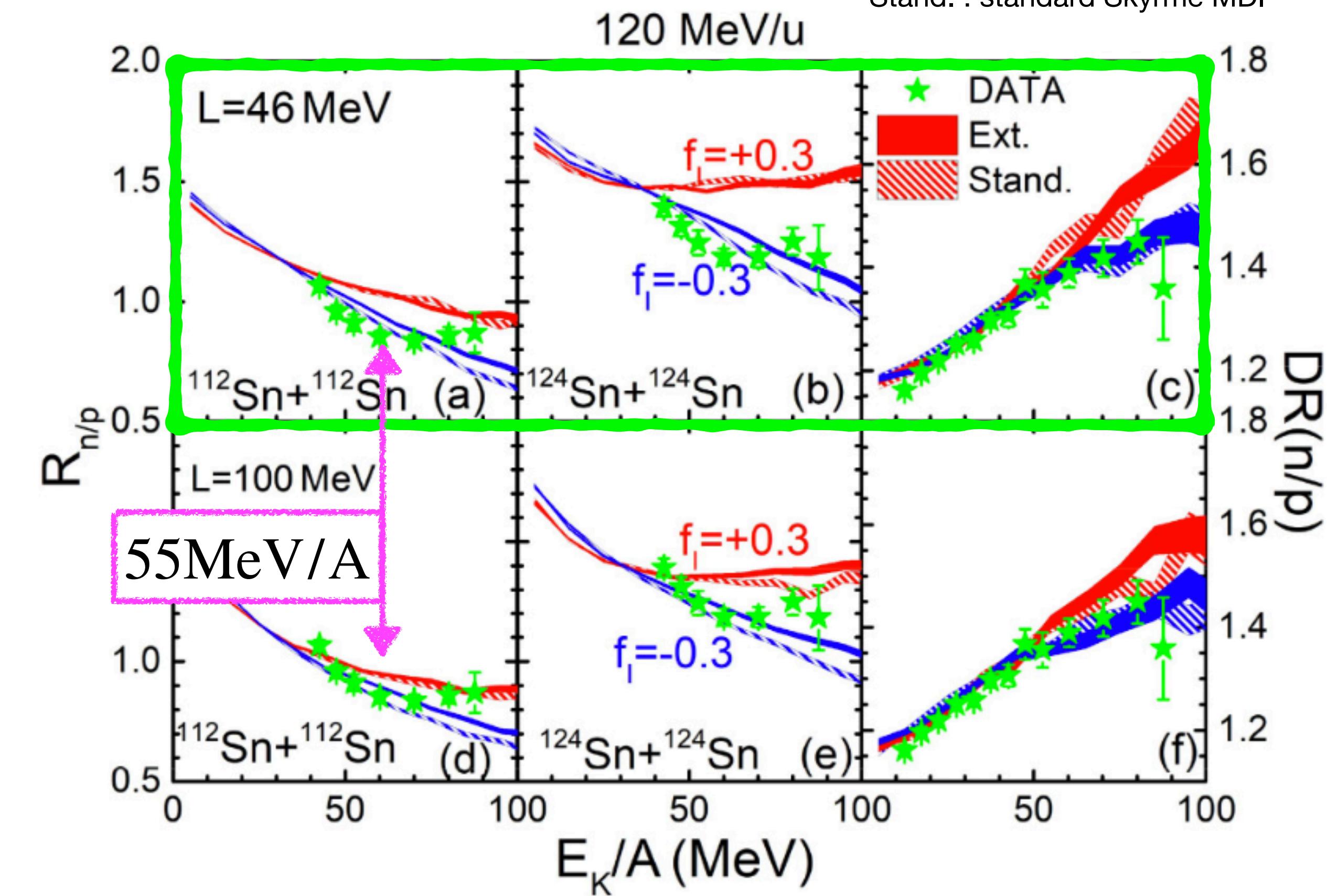
$$y_{cm}/y_{cm}^T \quad (y_{cm} < 0)$$

$$p_t^0 = \frac{p_t/A}{2p_t^P/(A_P + A_T)}$$

Parameter b : Offset of Elliptic flow



Ext. : extended Skyrme MDI
Stand. : standard Skyrme MDI



	K_{sym}	m^*/m	m_n^*/m	m_p^*/m
SLy4	-120	0.69	0.68	0.71
SkM*	-156	0.79	0.82	0.76

$$R_{n/p} = Y_{CI}(n)/Y_{CI}(p) \quad DR(n/p) = \frac{R(n/p, CI, 124)}{R(n/p, CI, 112)}$$

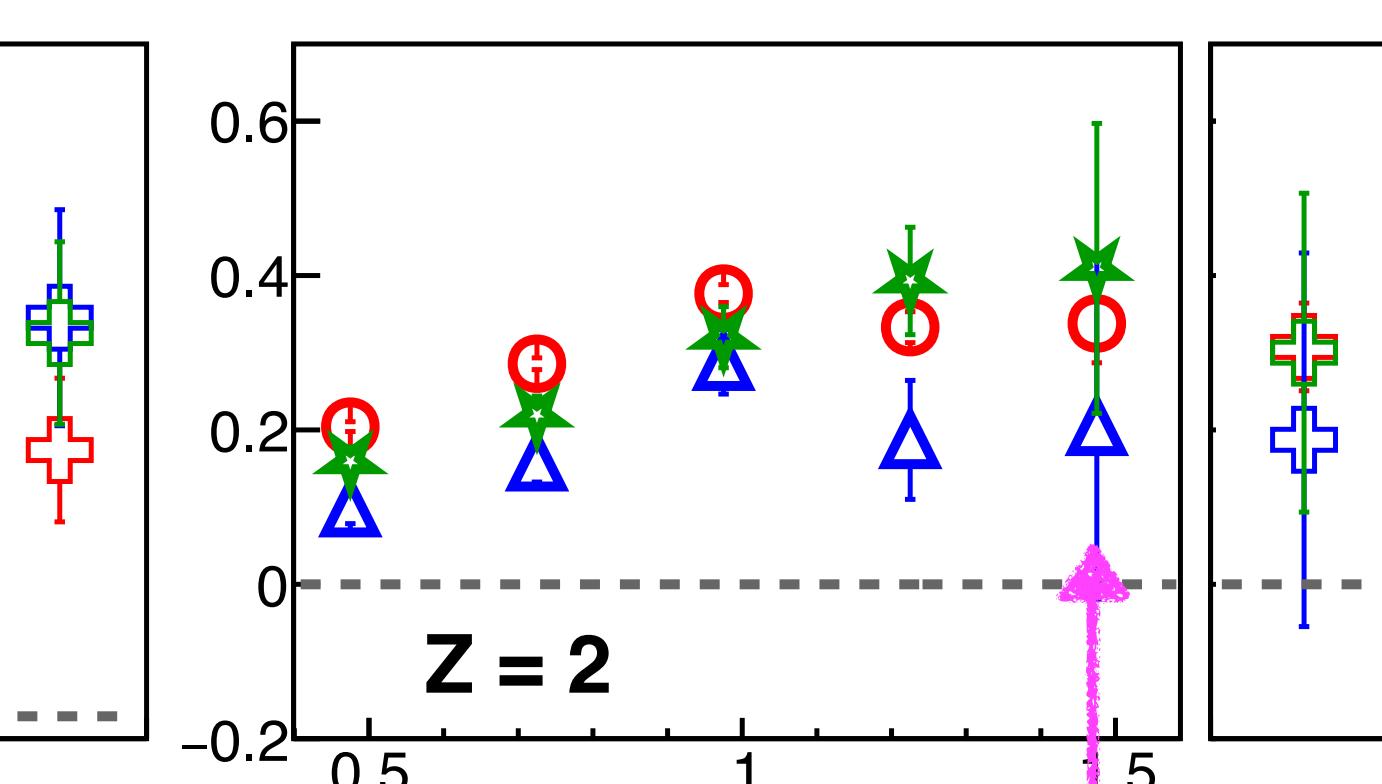
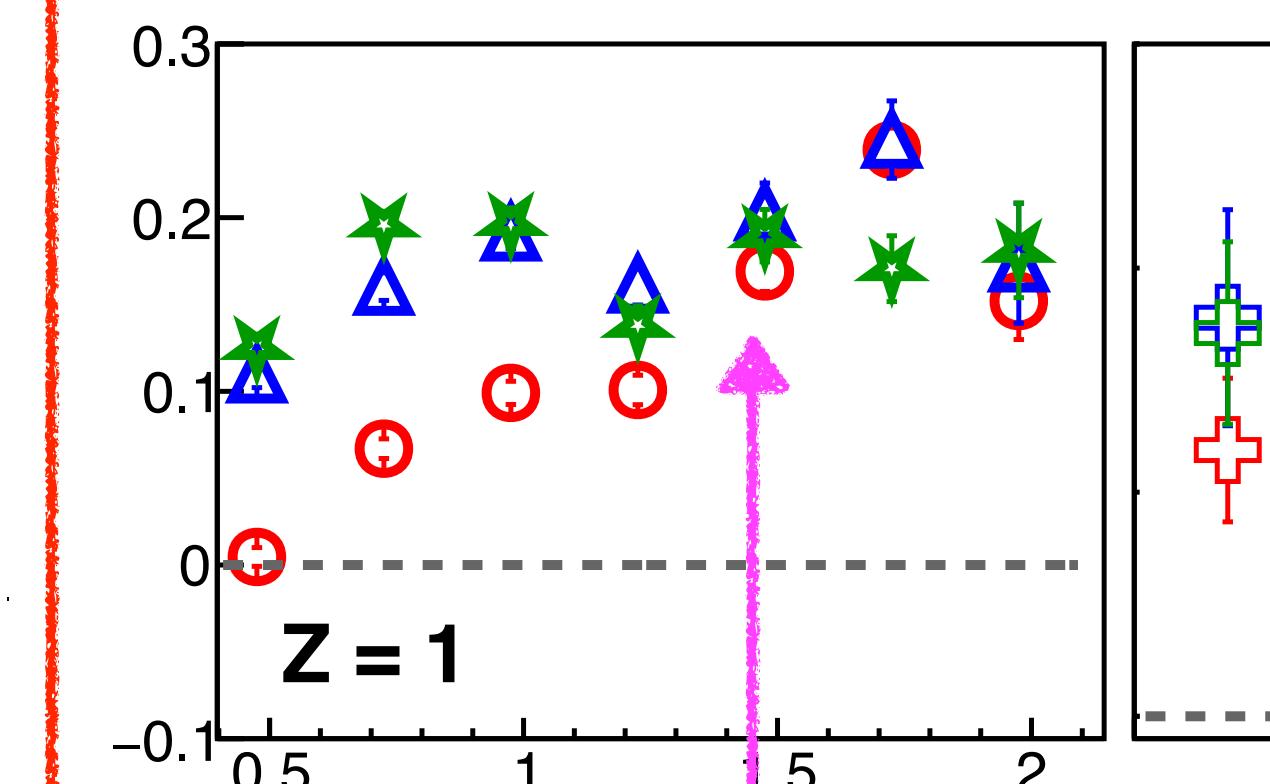
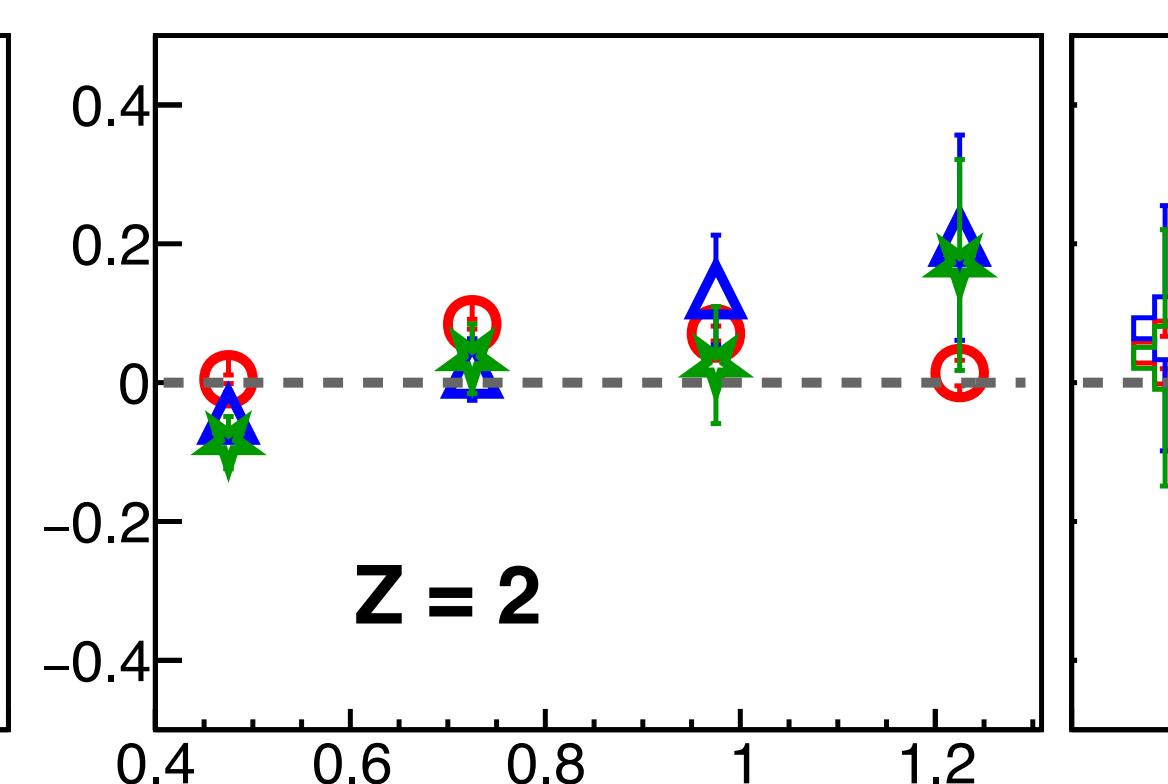
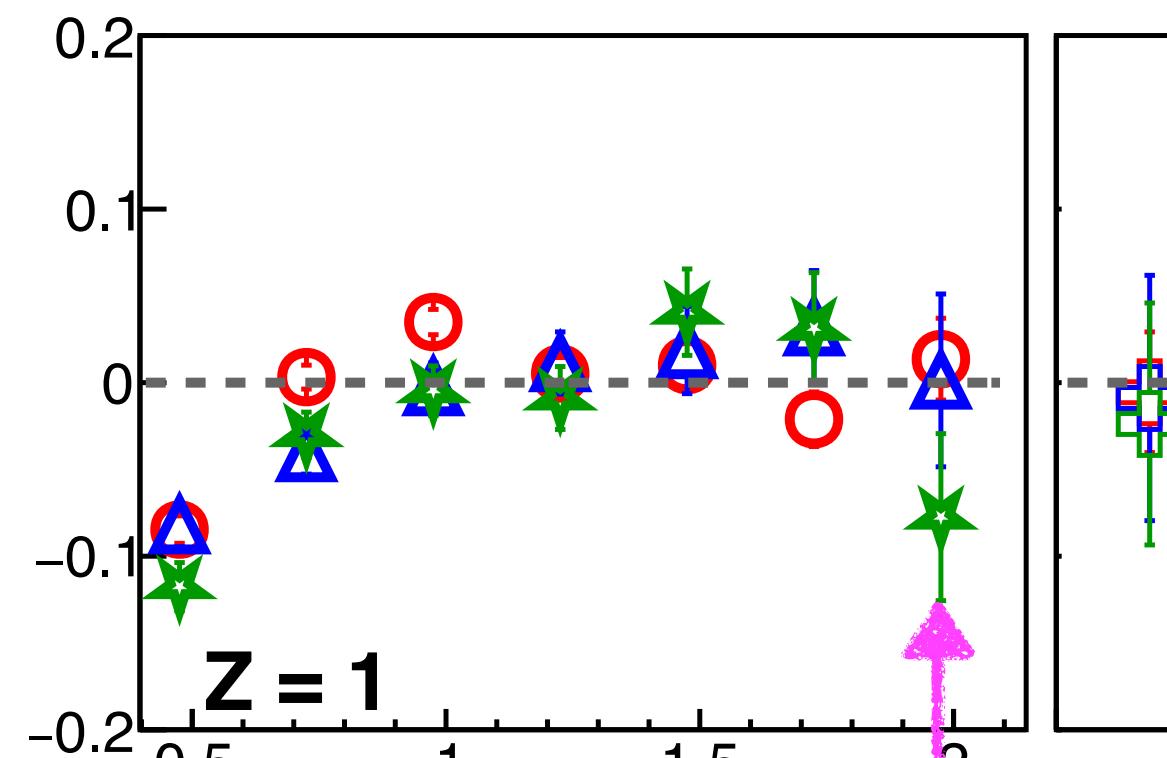
CI proton & neutron : $1 < A < 5$

$$f_I = 0.3(m_n^* < m_p^*)$$

$$f_I = -0.3(m_n^* > m_p^*)$$

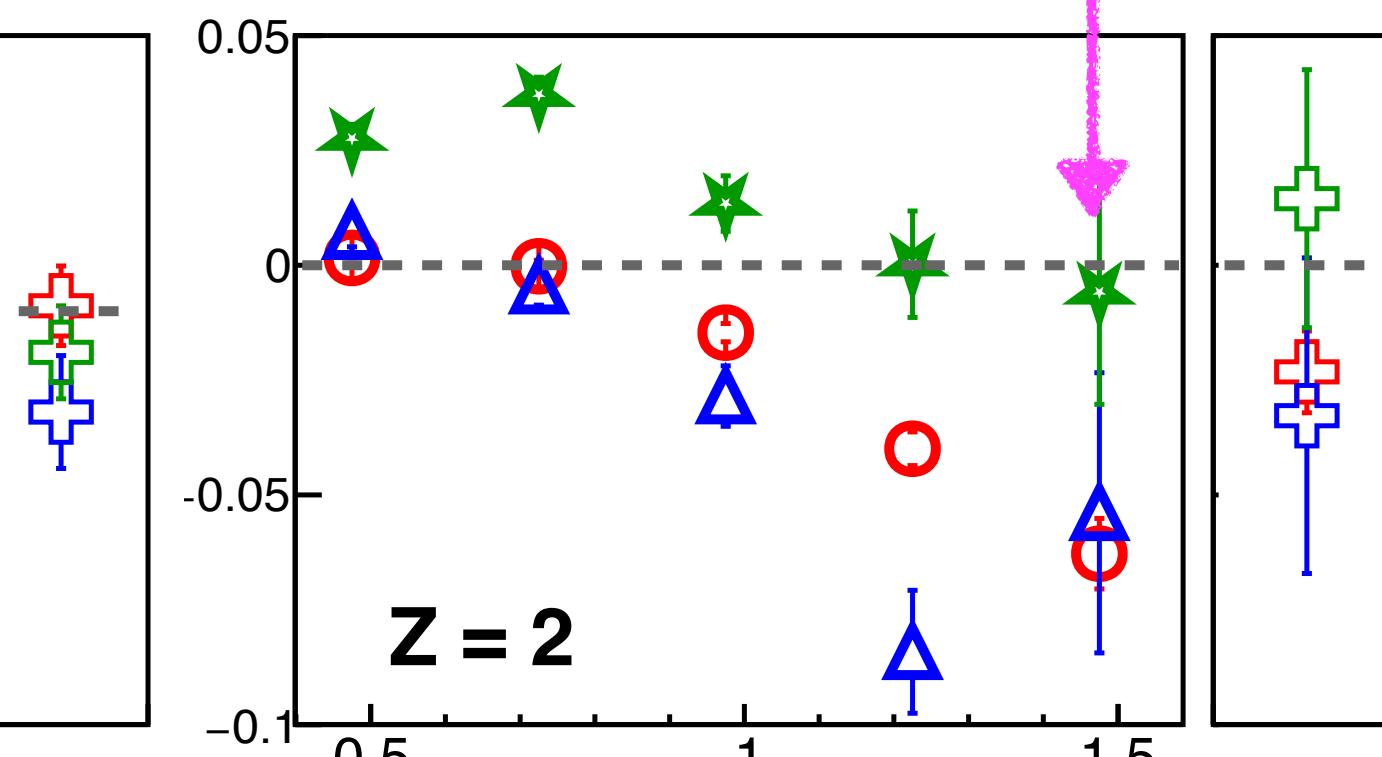
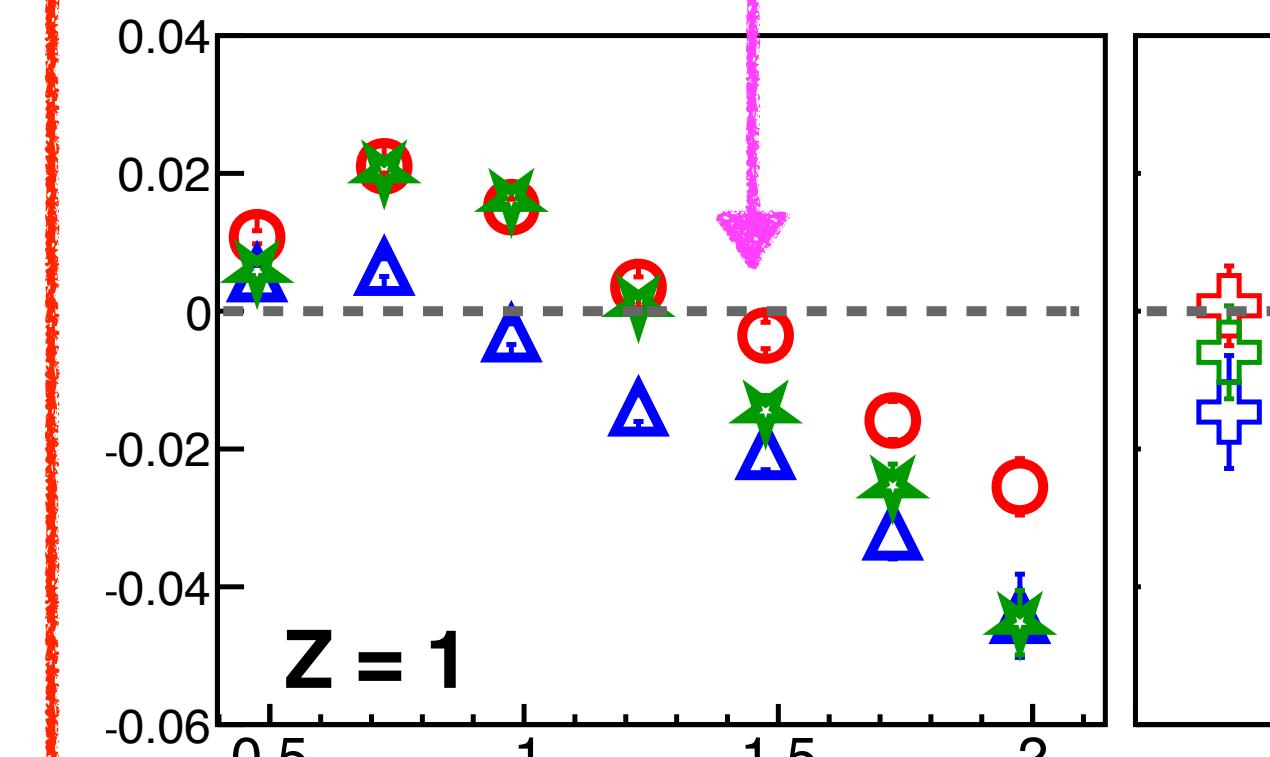
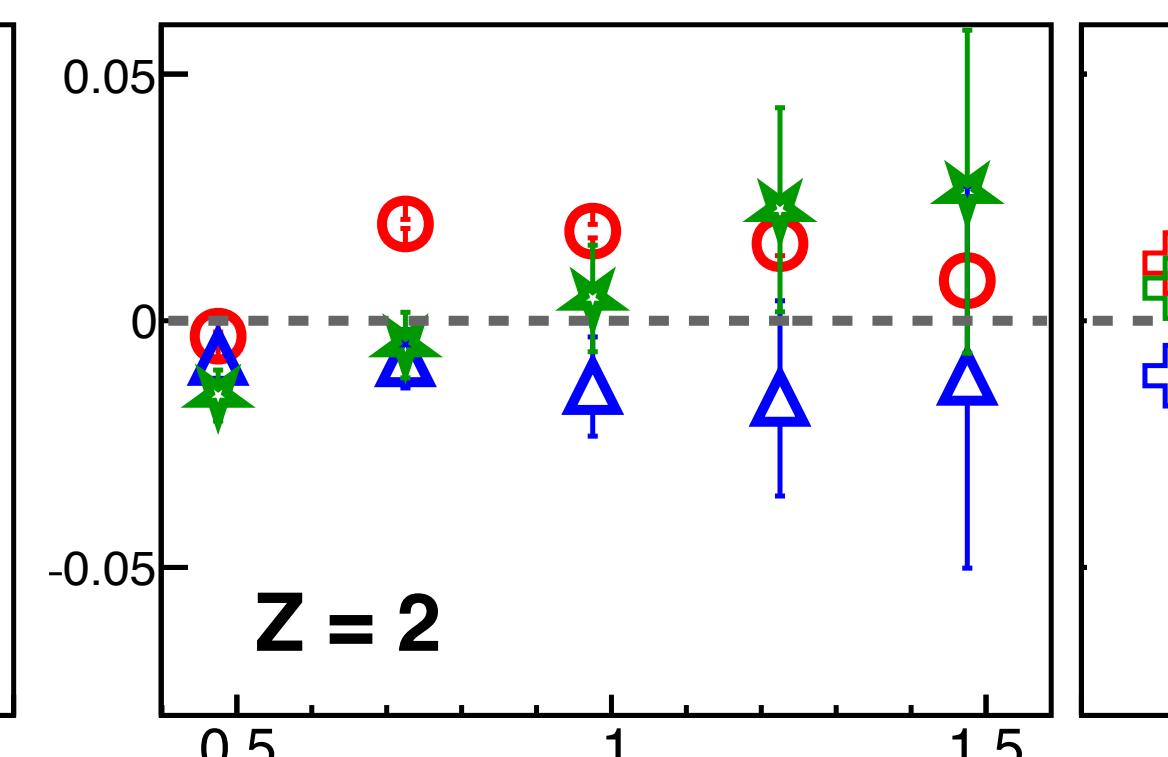
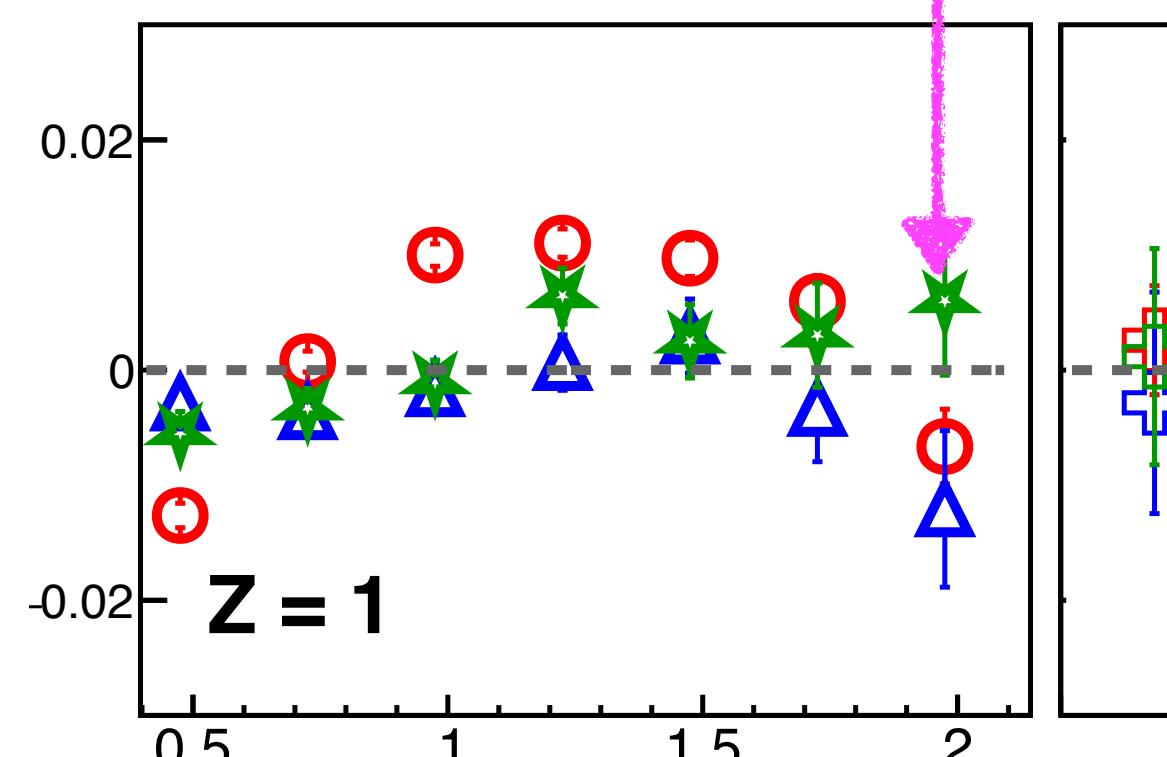
v₁ slope

With correction factor



EW1 Ni + Ni@ 52AMeV

IW1 Xe + Sn@ 100AMeV



$55 \text{ MeV/A} = p_t^0 \simeq 2.0$
for Ni + Ni@ 52AMeV

v₂ offset

$55 \text{ MeV/A} = p_t^0 \simeq 1.5$
for Xe + Sn@ 100AMeV

Slope of direct flow

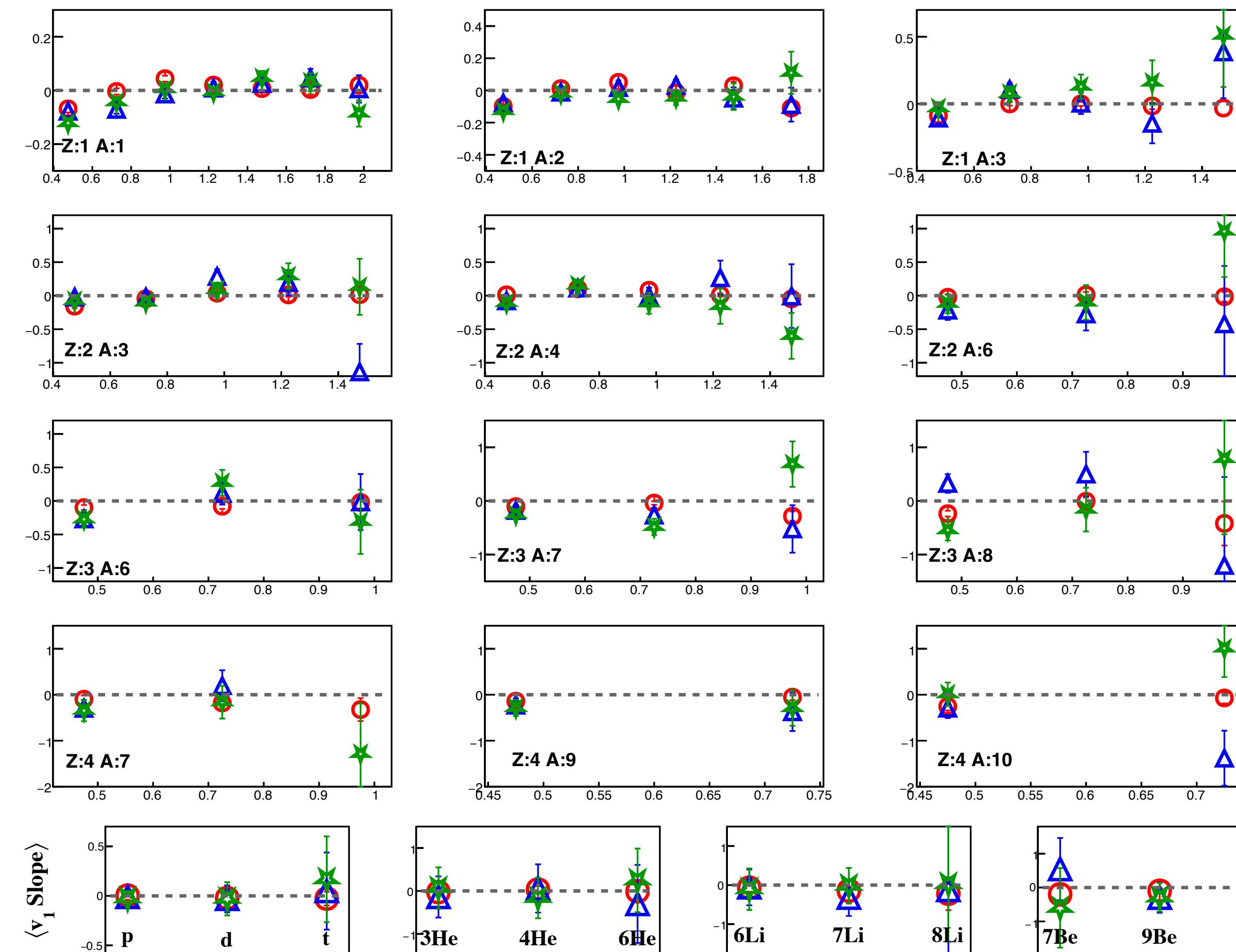
	K_{sym}	m^*/m	m_n^*/m	m_p^*/m
SLy4	-120	0.69	0.68	0.71
SkM*	-156	0.79	0.82	0.76

$^{64}\text{Ni} + ^{64}\text{Ni}$ @ 52MeV/u

$^{124}\text{Xe} + ^{124}\text{Sn}$ @ 100MeV/u
With correction factor

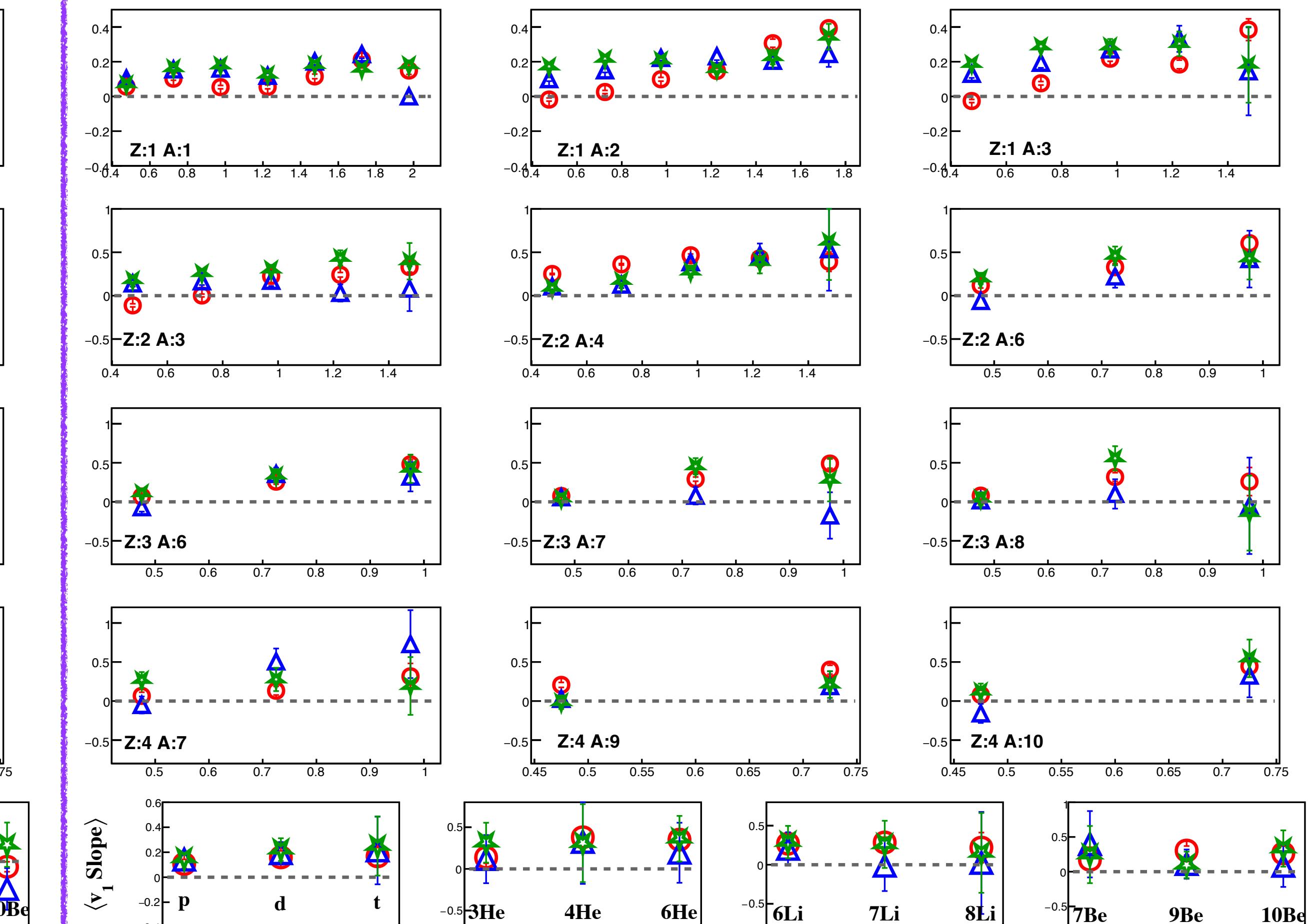
EW1 p_t^0 vs v_1 Slope

○ Exp ▲ SLy4 ★ SkMs



IW1 p_t^0 vs v_1 Slope

○ Exp ▲ SLy4 ★ SkMs



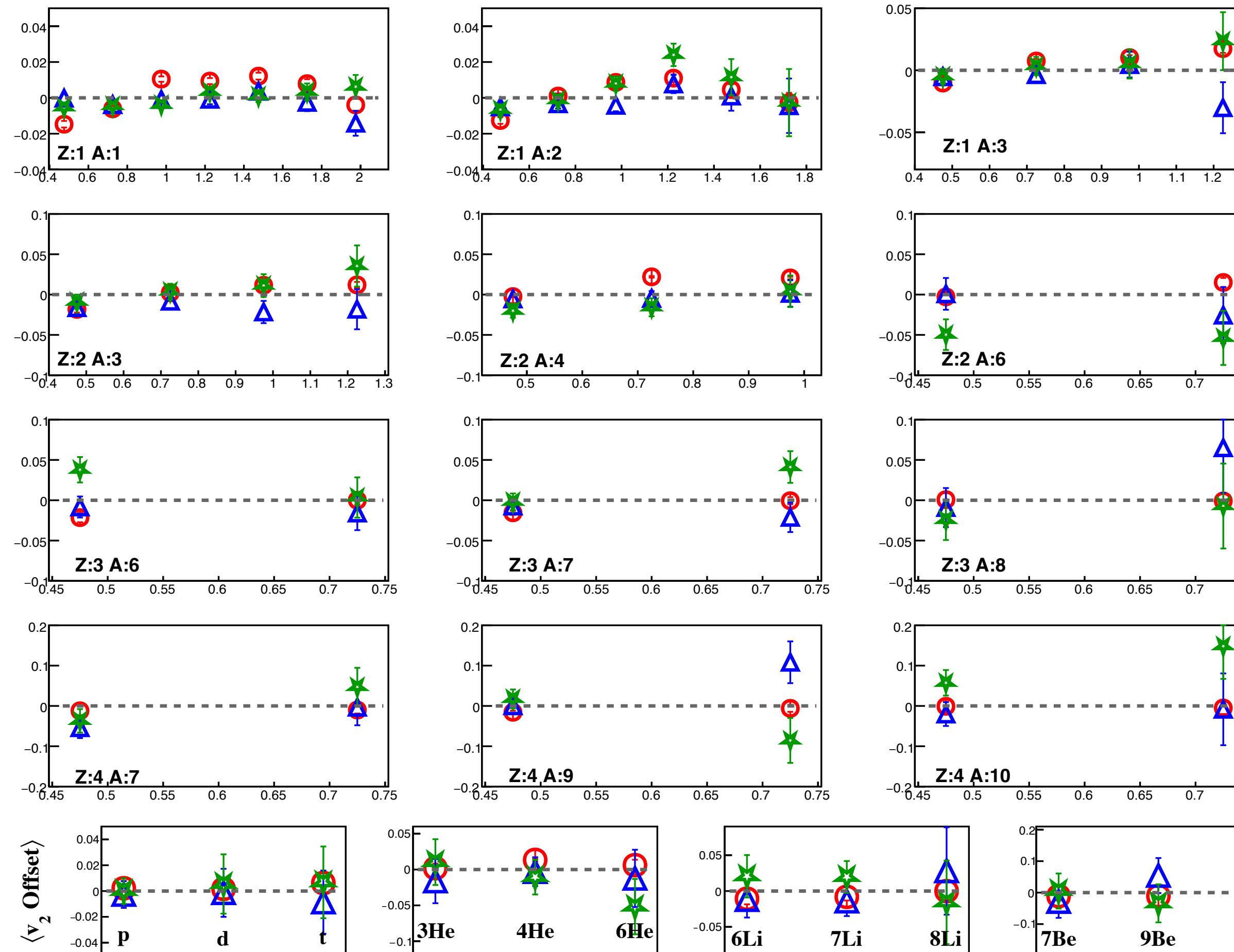
Offset of Elliptic flow

	K_{sym}	m^*/m	m_n^*/m	m_p^*/m
SLy4	-120	0.69	0.68	0.71
SkM*	-156	0.79	0.82	0.76

$^{64}\text{Ni} + ^{64}\text{Ni}$ @ 52MeV/u

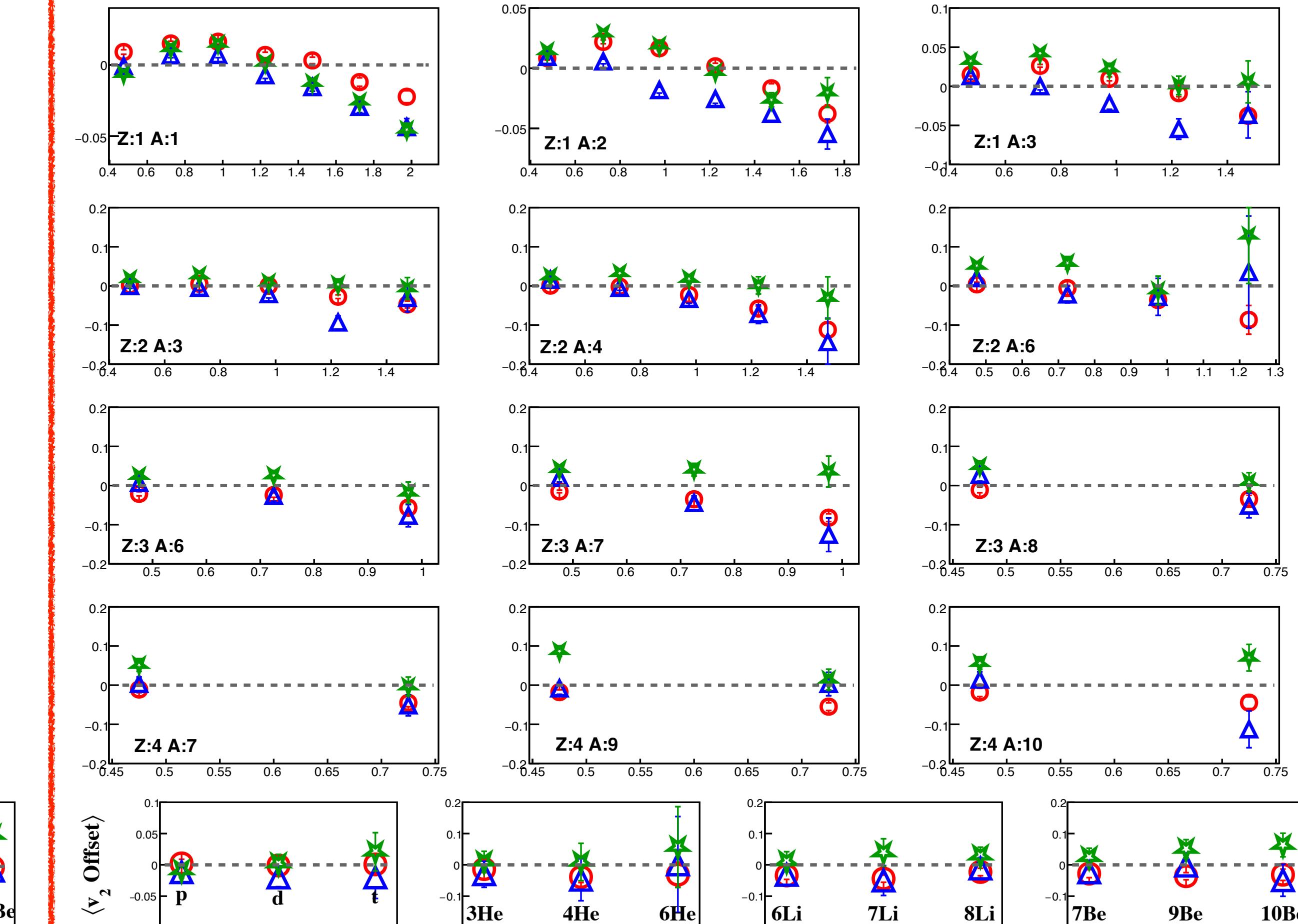
EW1 p_t^0 vs v_2 Offset

○ Exp ▲ SLy4 ★ SkMs

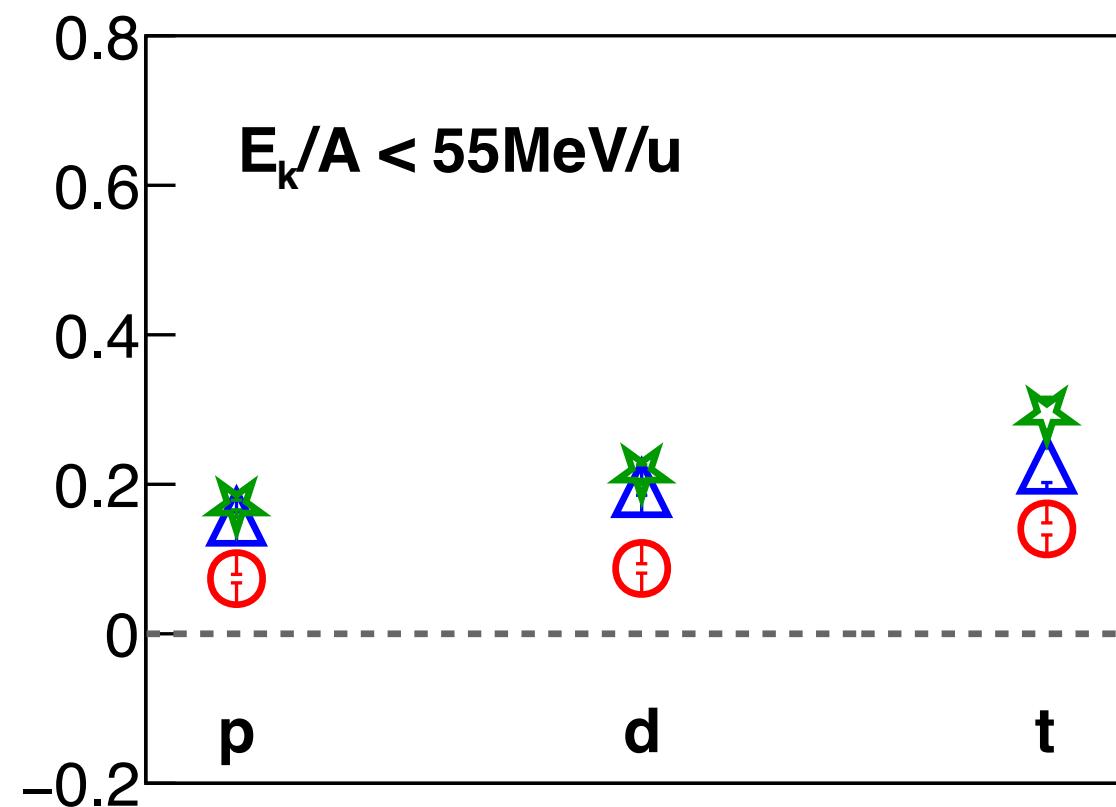
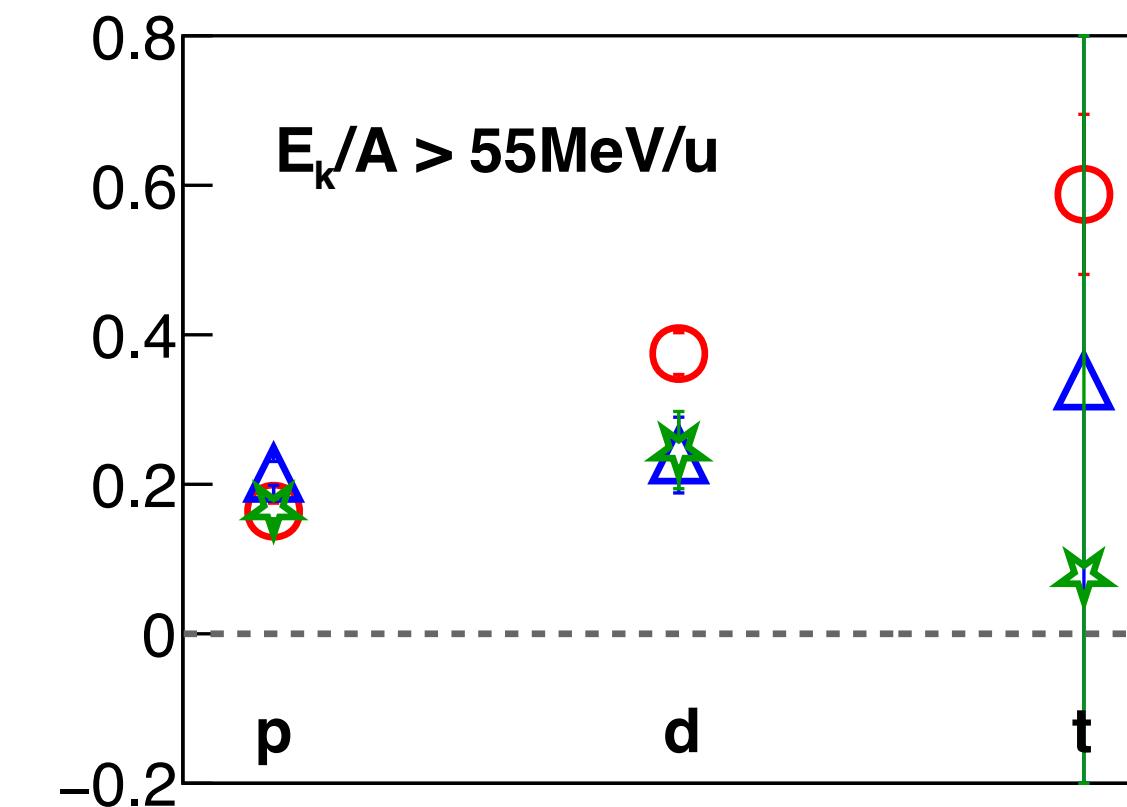
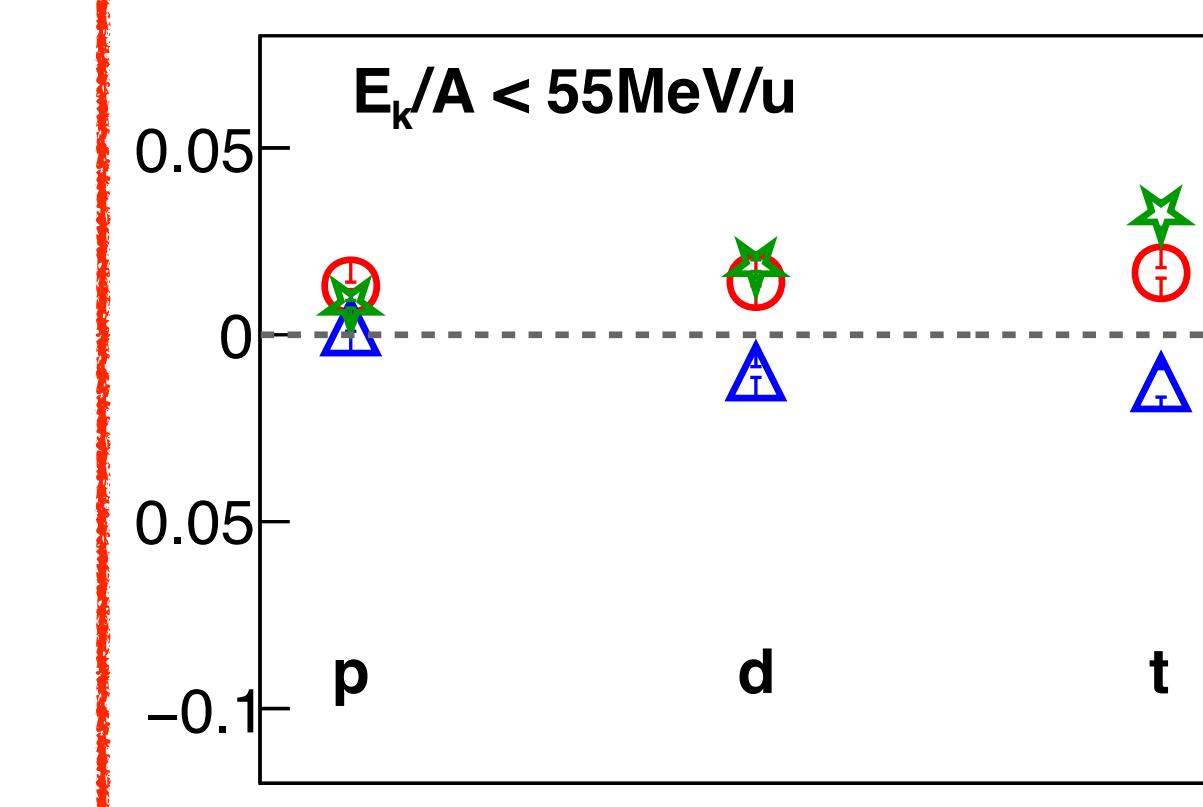
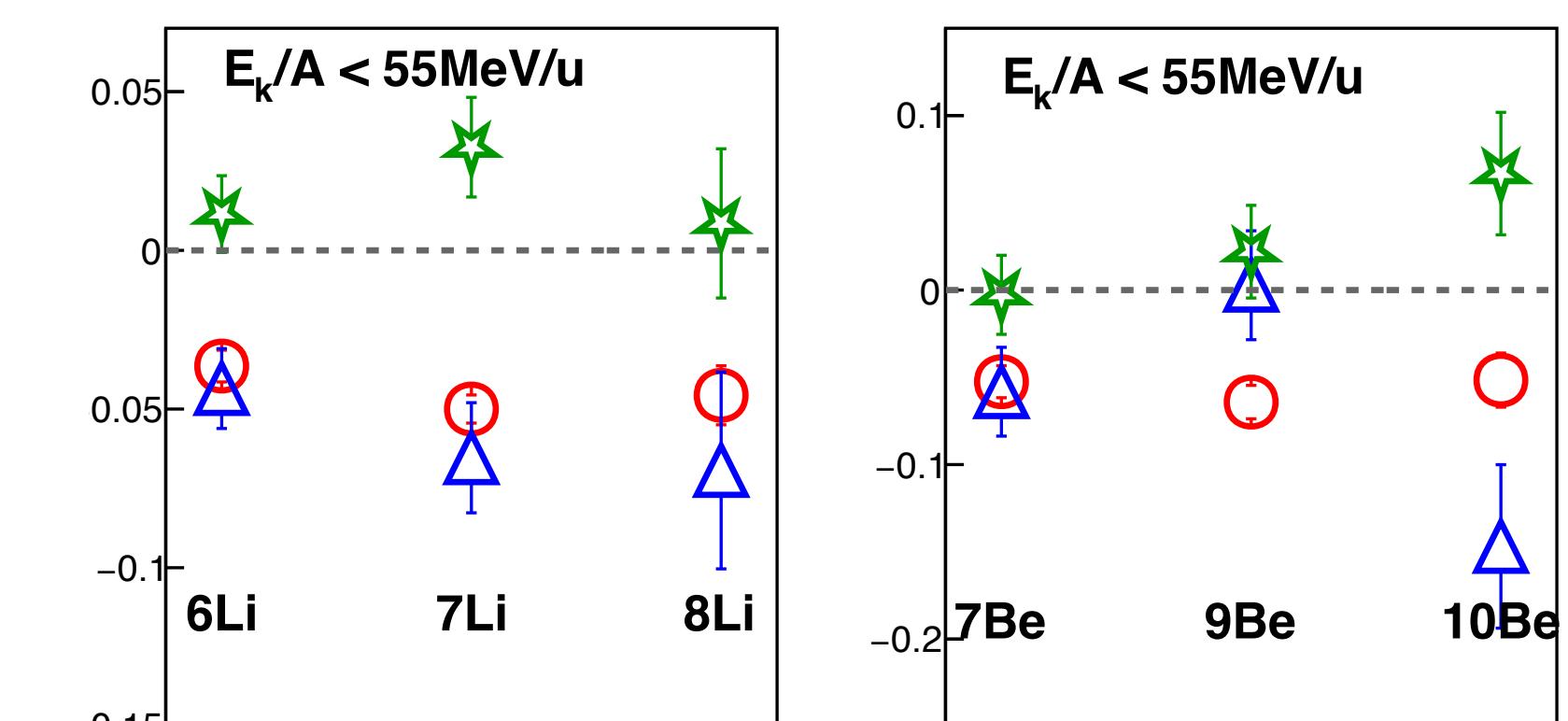
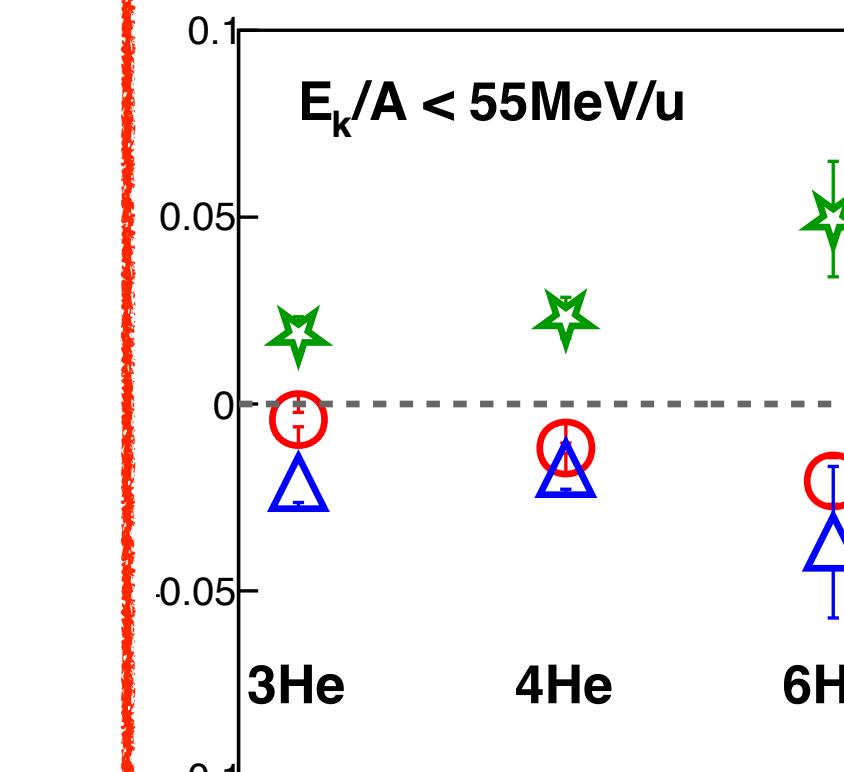
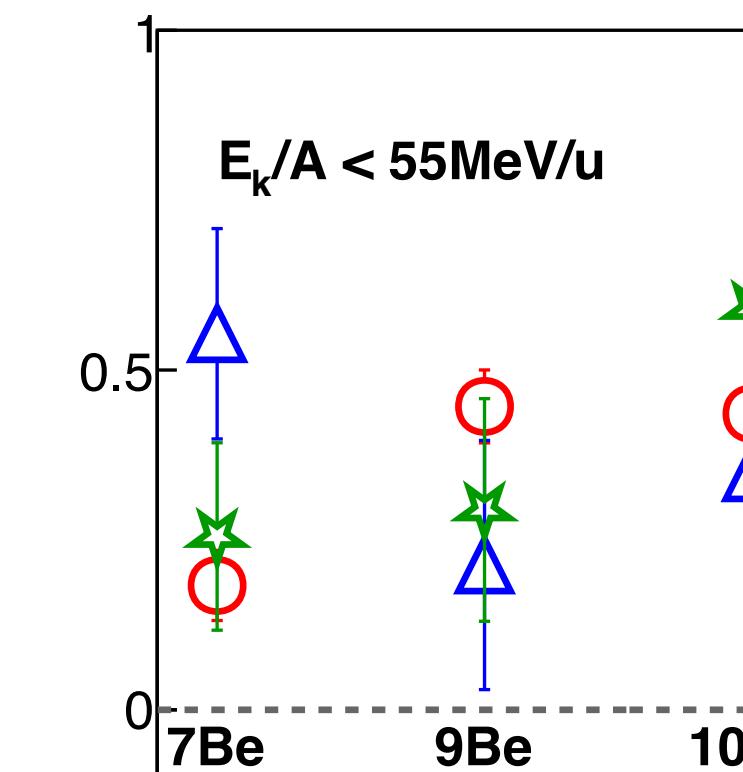
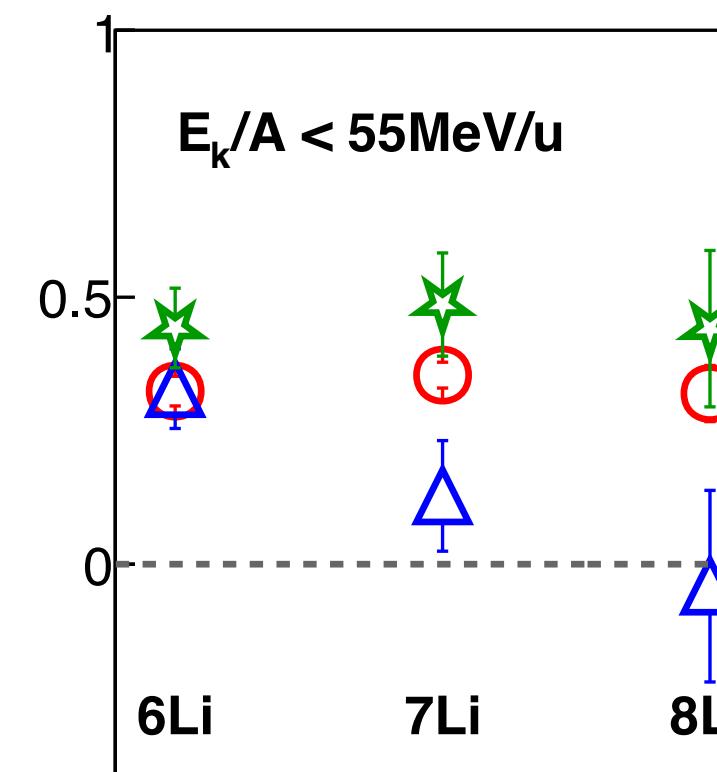
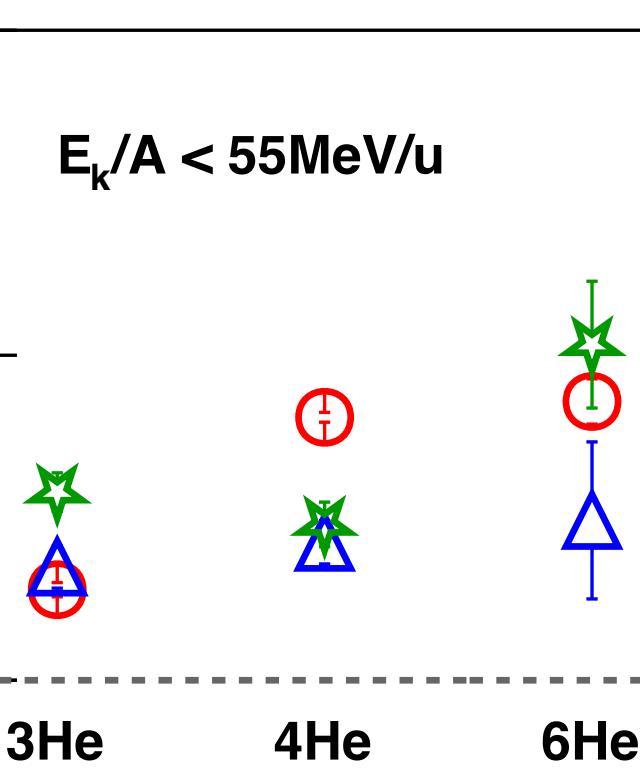
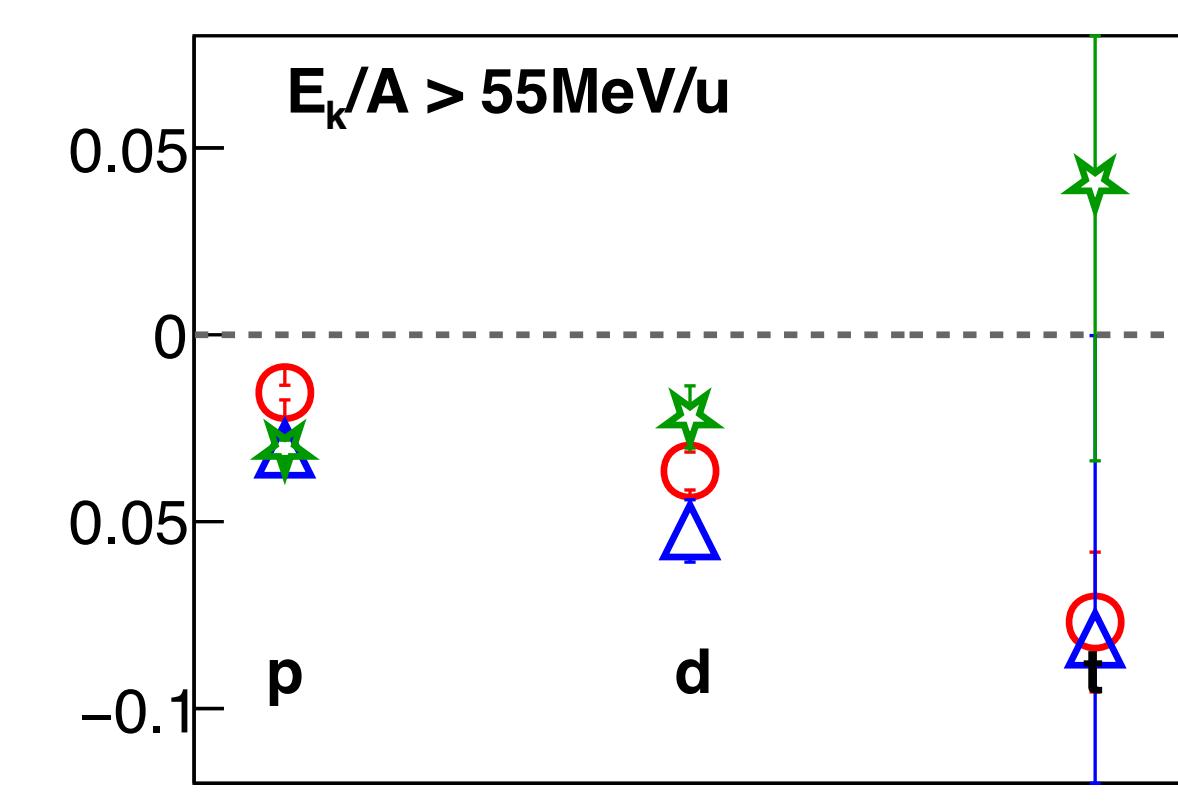


IW1 p_t^0 vs v_2 Offset

○ Exp ▲ SLy4 ★ SkMs



With correction factor

IW1 isotope vs v_1 SlopeIW1 isotope vs v_1 SlopeIW1 isotope vs v_2 OffsetIW1 isotope vs v_2 Offset

Summary

1. Compare Experimental and ImQMD with 2 Skyrme parameters data using v_1 slope and v_2 offset.
2. v_1 and v_2 results of two model calculation using Ni+Ni @ 52 AMeV are not show clear difference and also models can not predict experimental results.
3. v_1 of Xe+Sn @ 100 AMeV from two parameter sets are not show specific difference relate to N/Z of fragment and also non of model predict experimental result especially at low p_t^0 regions.
4. v_2 from 2 parameters of Xe+Sn @ 100AMeV are represent clearly differences and this are affected by N/Z ratio of fragments.

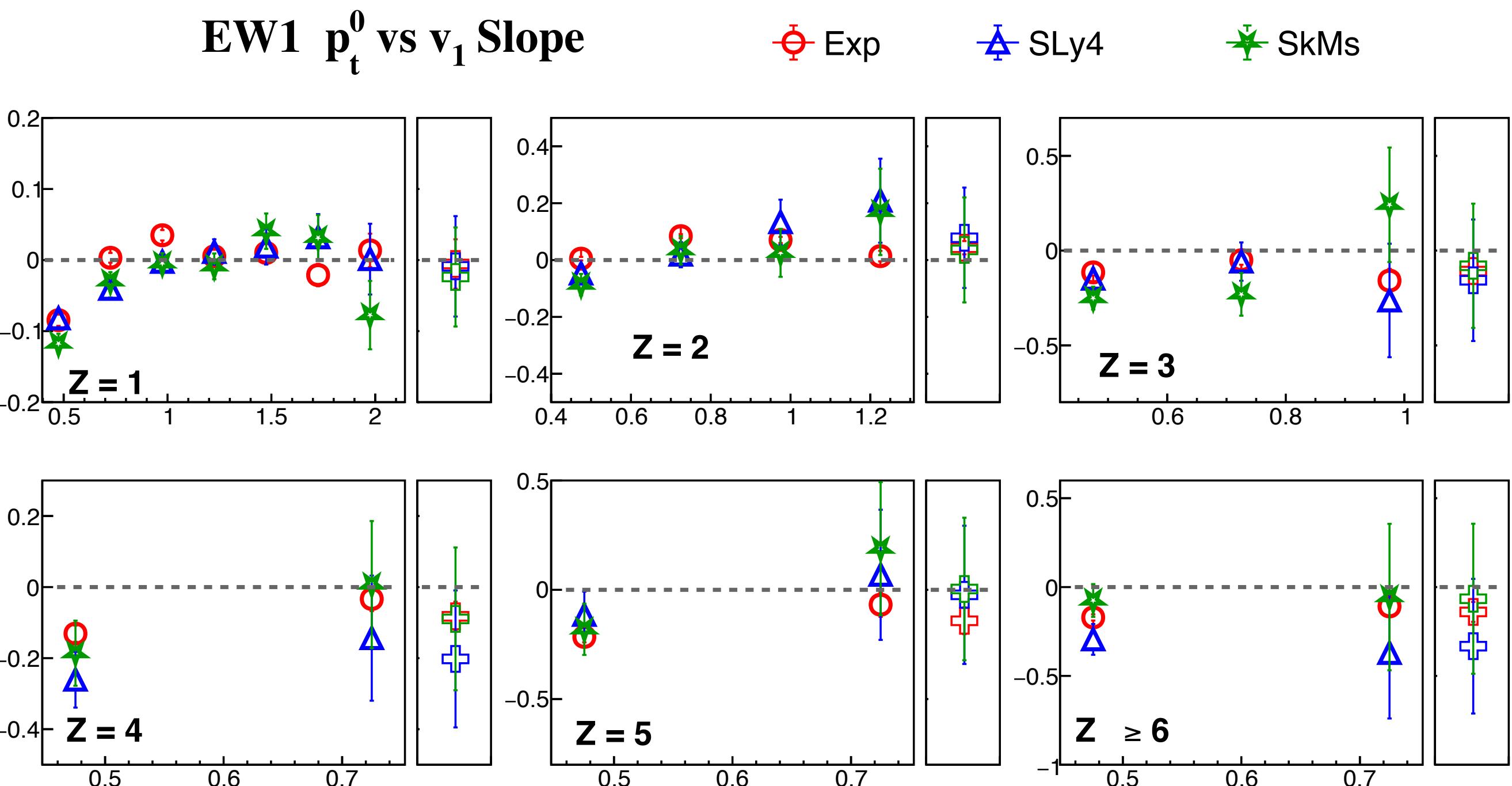
Conclusion

1. Direct flow seems not sensitive to iso-vector effective mass difference.
2. Elliptic flow is more sensitive to iso-vector effective mass splitting of proton and neutron but direct flow is not in this energy region.
3. Effective mass of proton much heavier than value of SkM* at over $E_k \sim 55\text{MeV/u}$ but little heavier below $E_k \sim 55\text{MeV/u}$.
4. Effective mass of neutron is lighter than SkM* and heavier than SLy4 at below $E_k \sim 55\text{MeV/u}$.

Backup

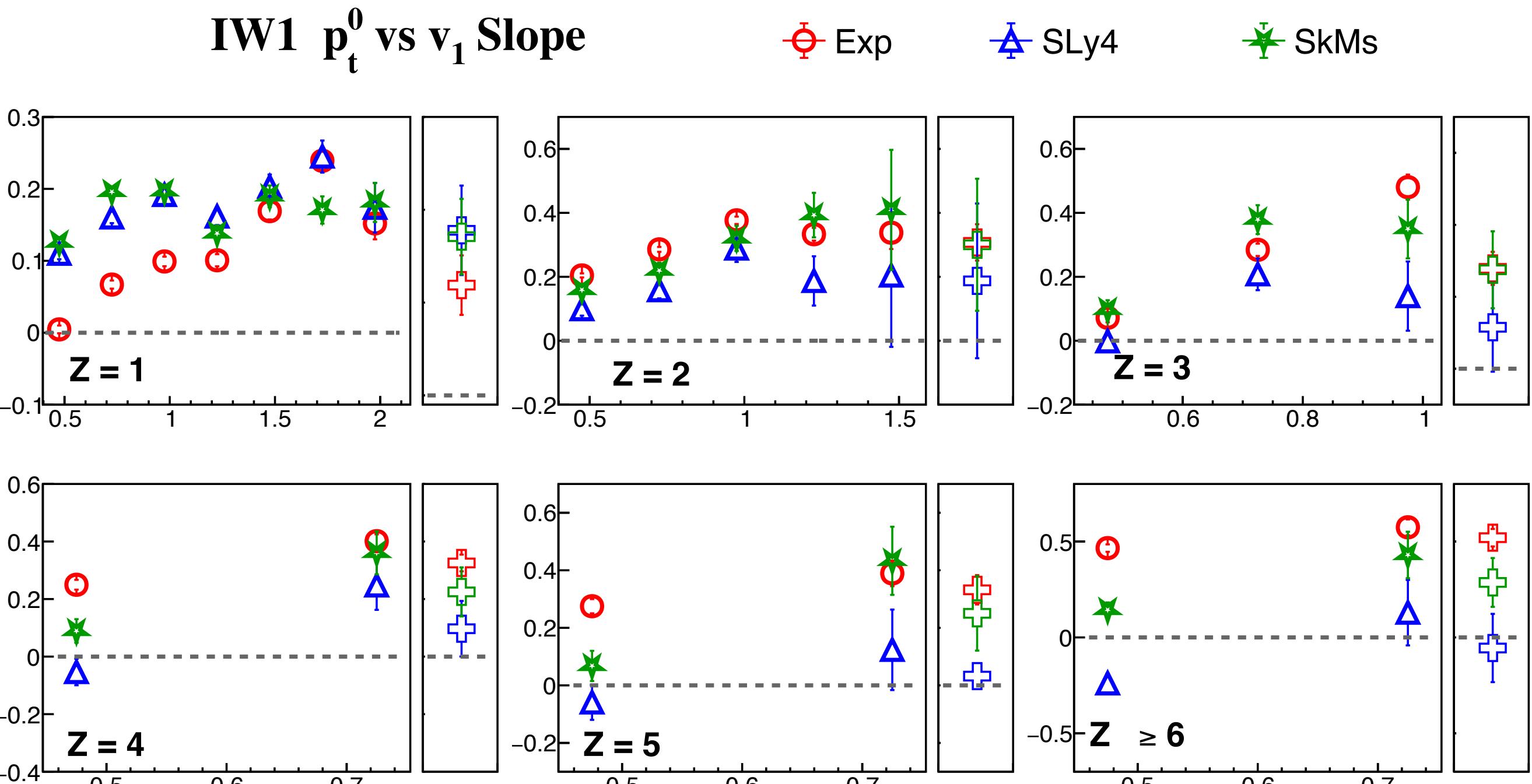
Slope of Direct flow

$^{64}\text{Ni} + ^{64}\text{Ni}$ @ 52MeV/u



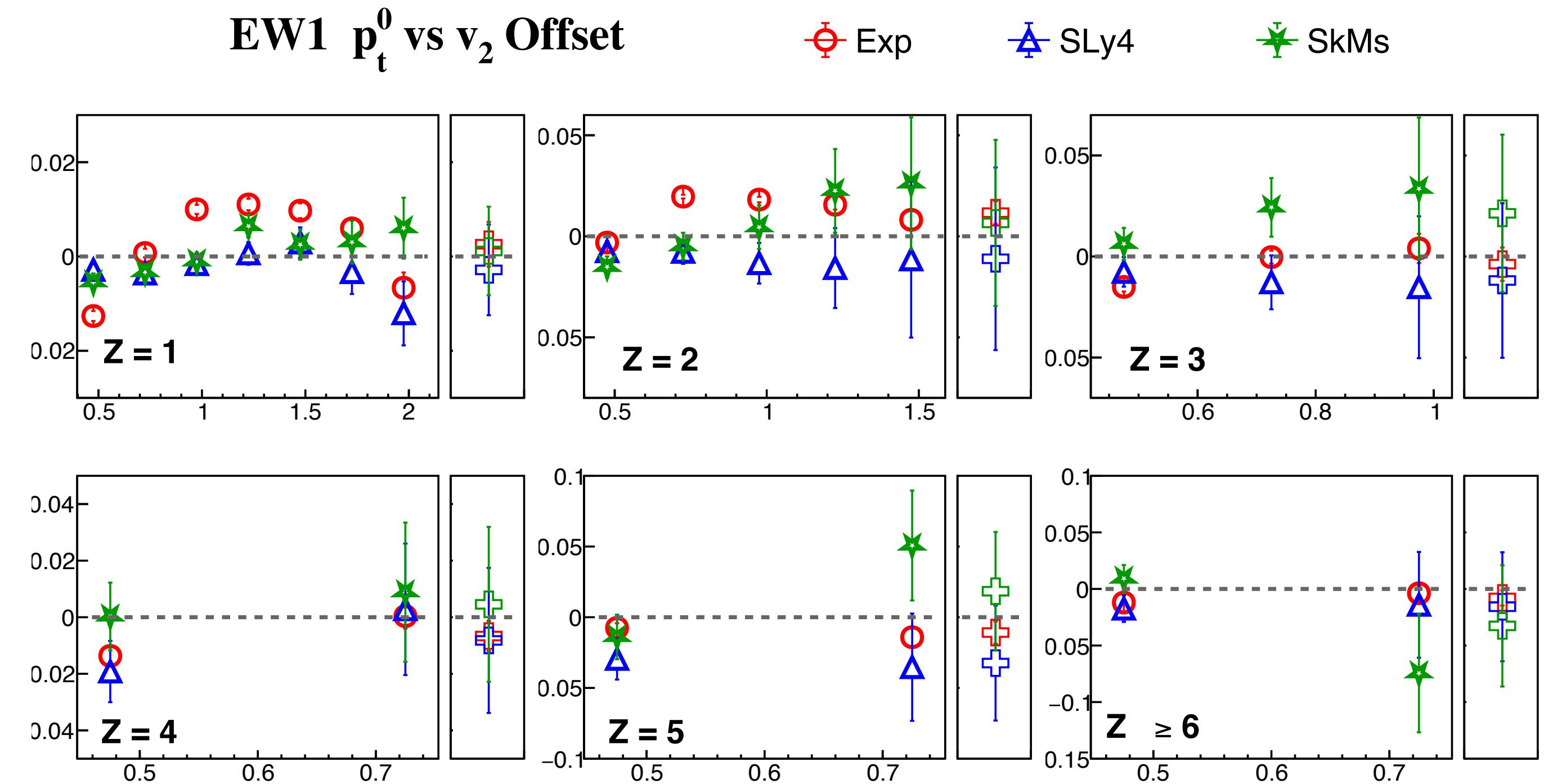
$^{124}\text{Xe} + ^{124}\text{Sn}$ @ 100MeV/u

With correction factor



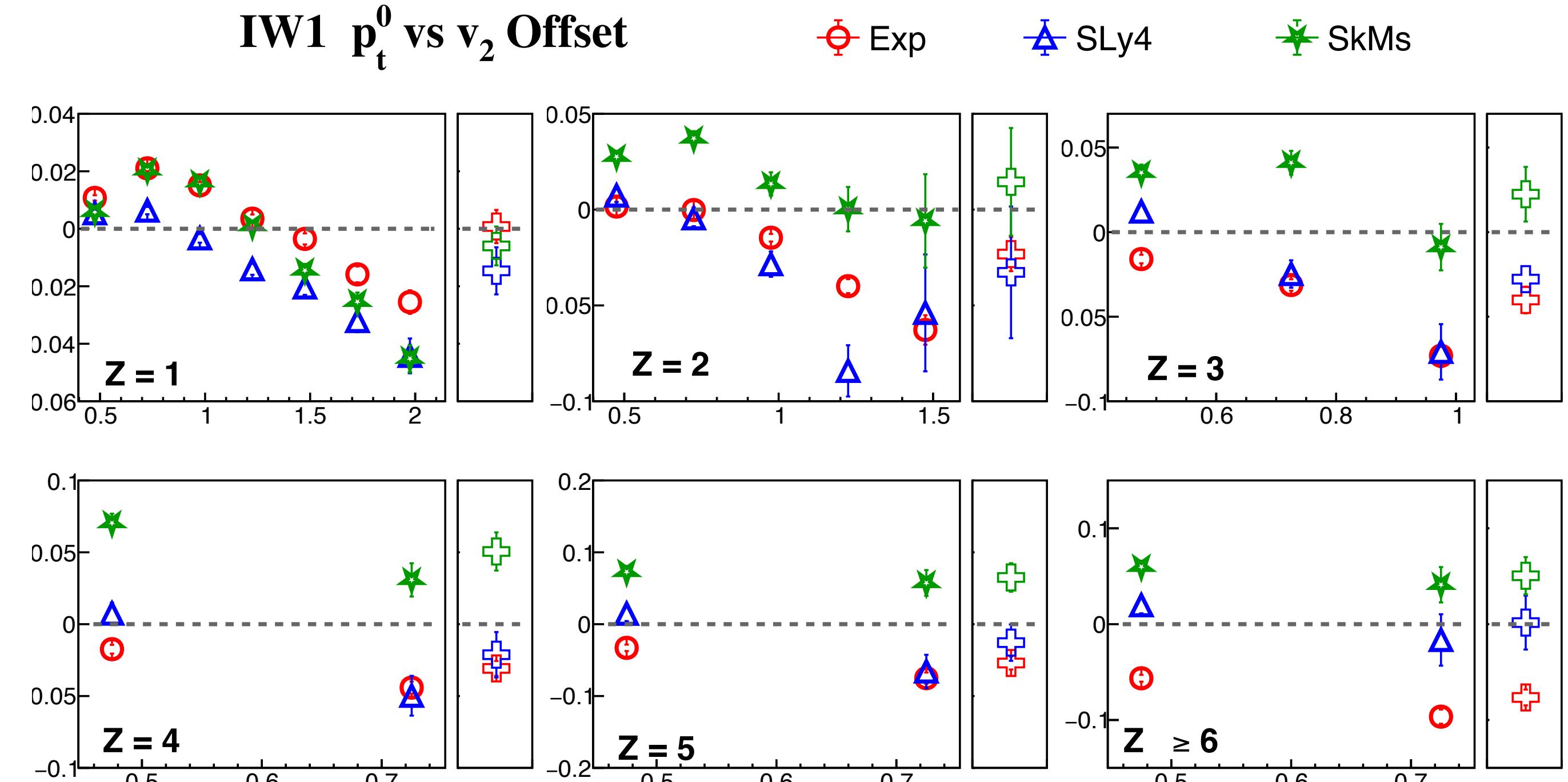
Offset of Elliptic flow

$^{64}\text{Ni} + ^{64}\text{Ni}$ @ 52MeV/u

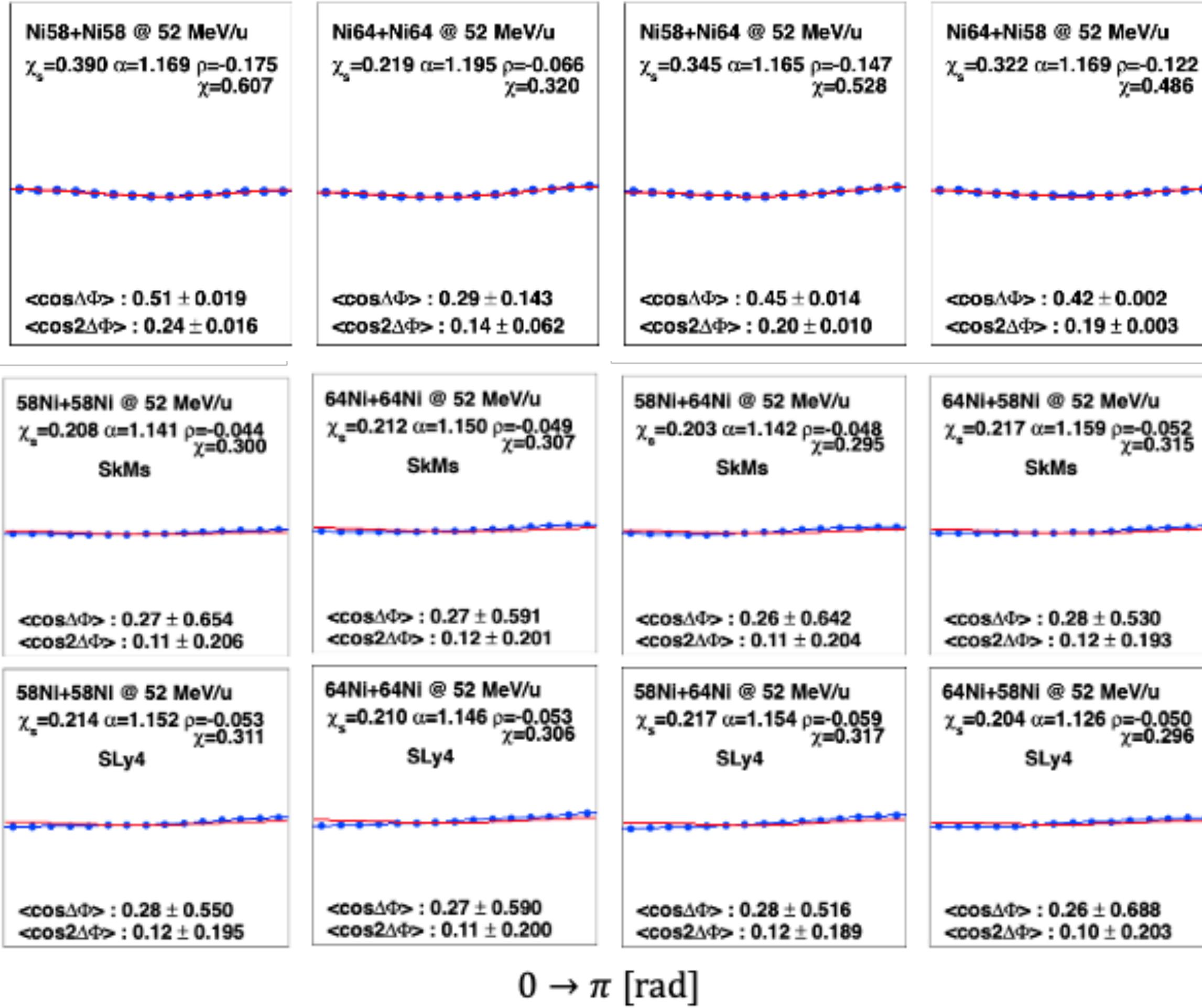


$^{124}\text{Xe} + ^{124}\text{Sn}$ @ 100MeV/u

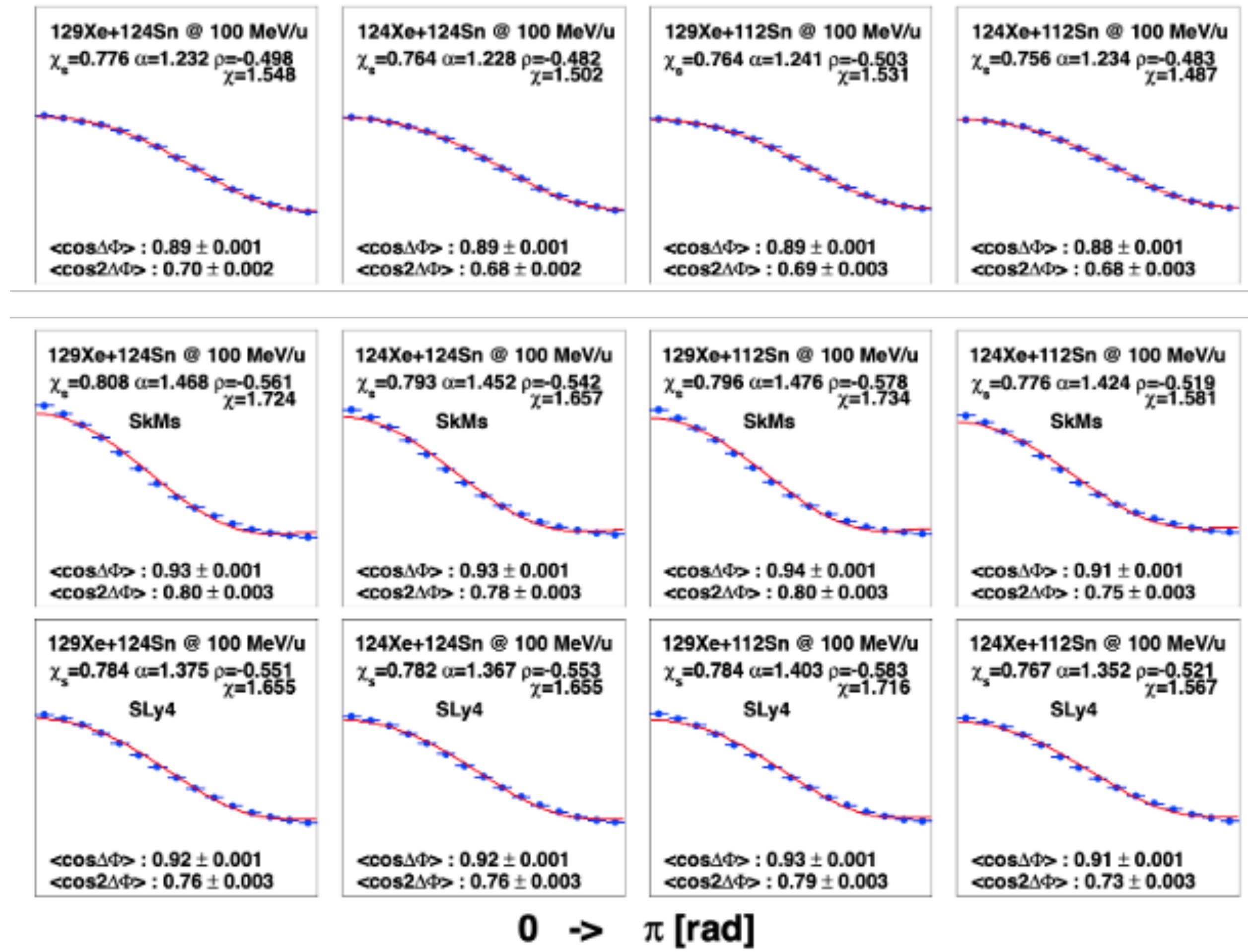
With correction factor



$^{64,58}\text{Ni} + ^{64,58}\text{Ni}$ @ 52MeV/u

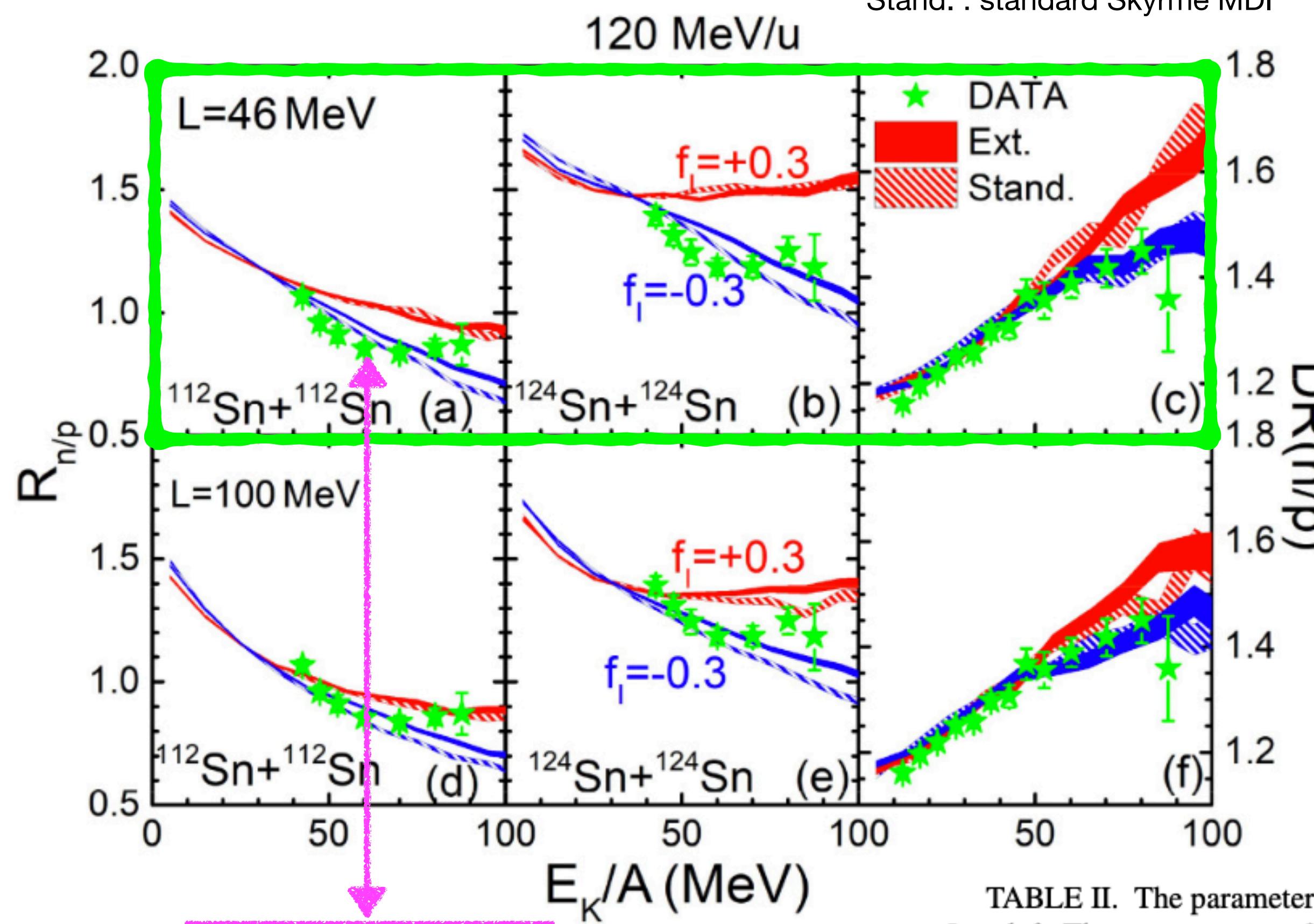


$^{129,124}\text{Xe} + ^{124,112}\text{Sn}$ @ 100MeV/u



Ext. : extended Skyrme MDI

Stand. : standard Skyrme MDI



55MeV/A

$$f_I = 0.3(m^*_n < m^*_p)$$

$$f_I = -0.3(m^*_n > m^*_p)$$

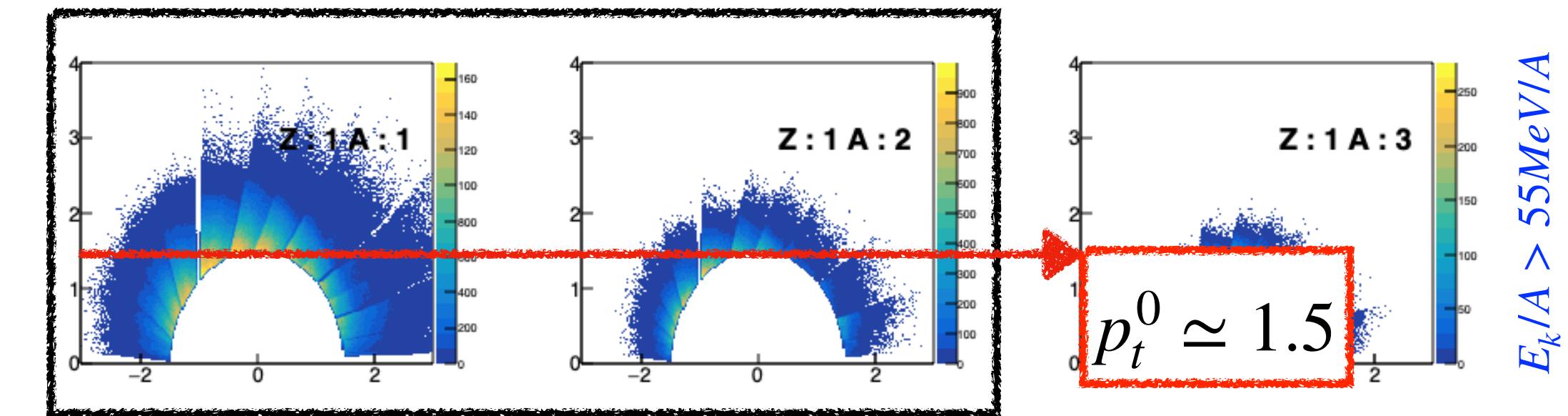
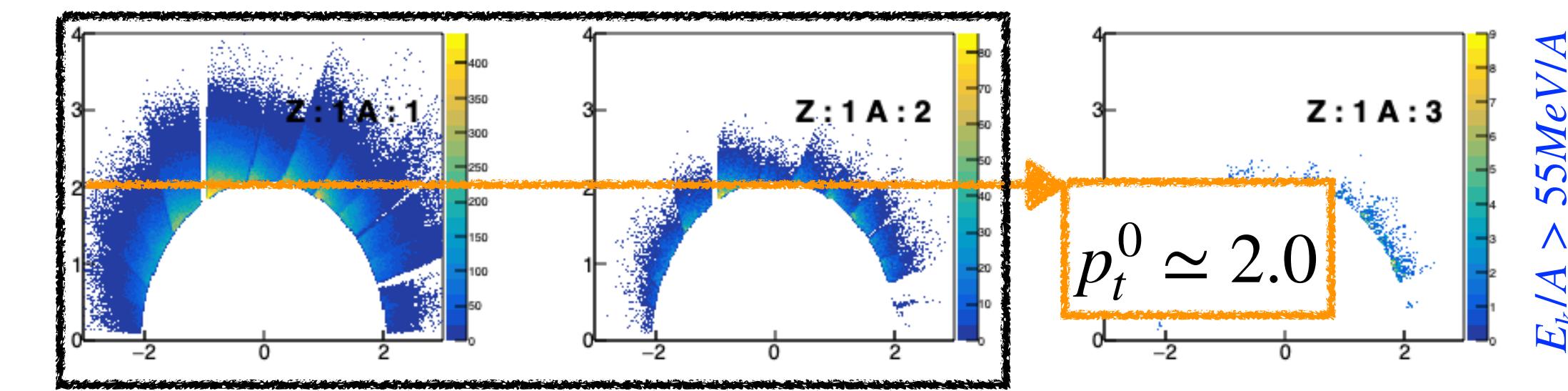
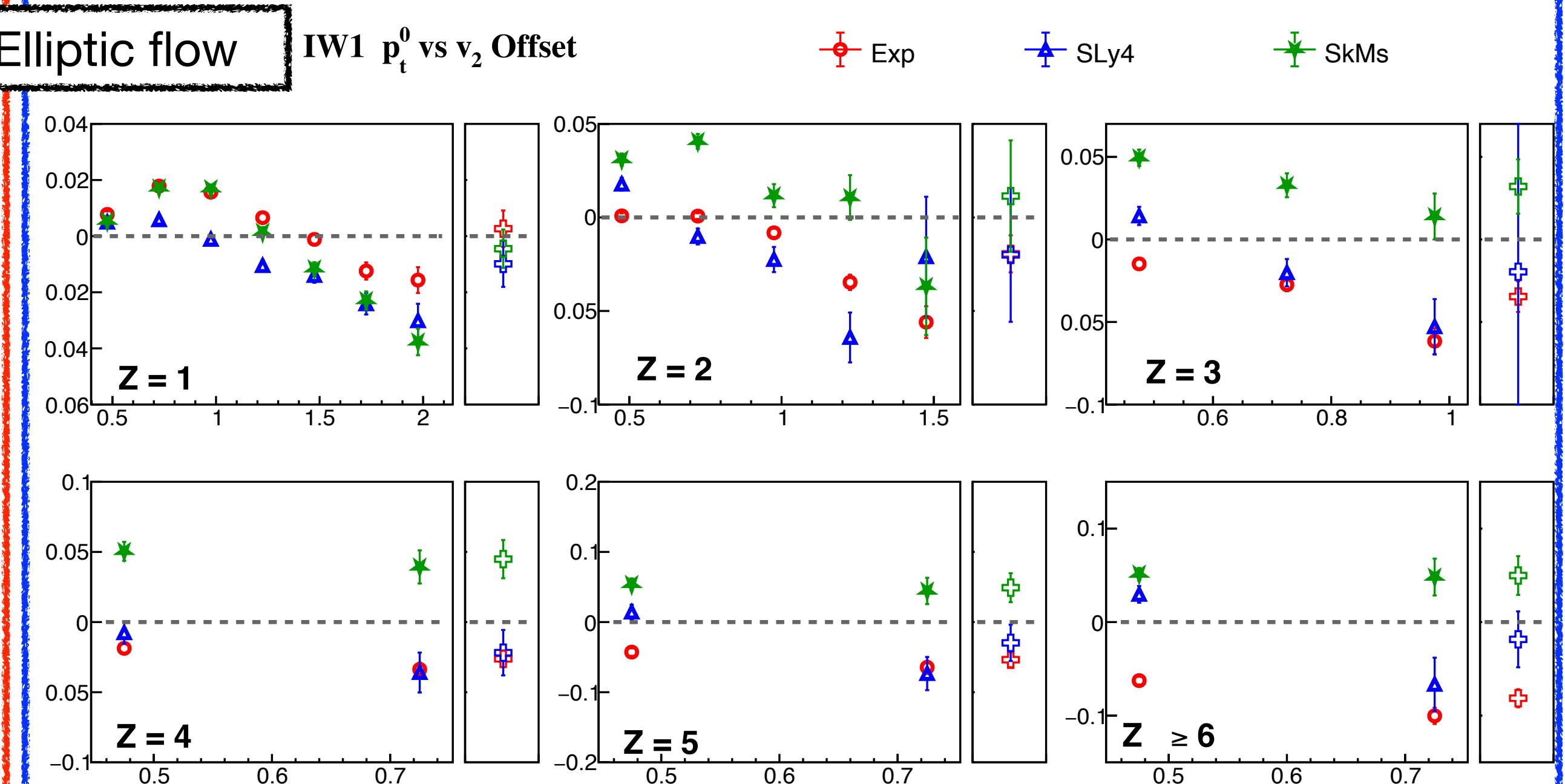
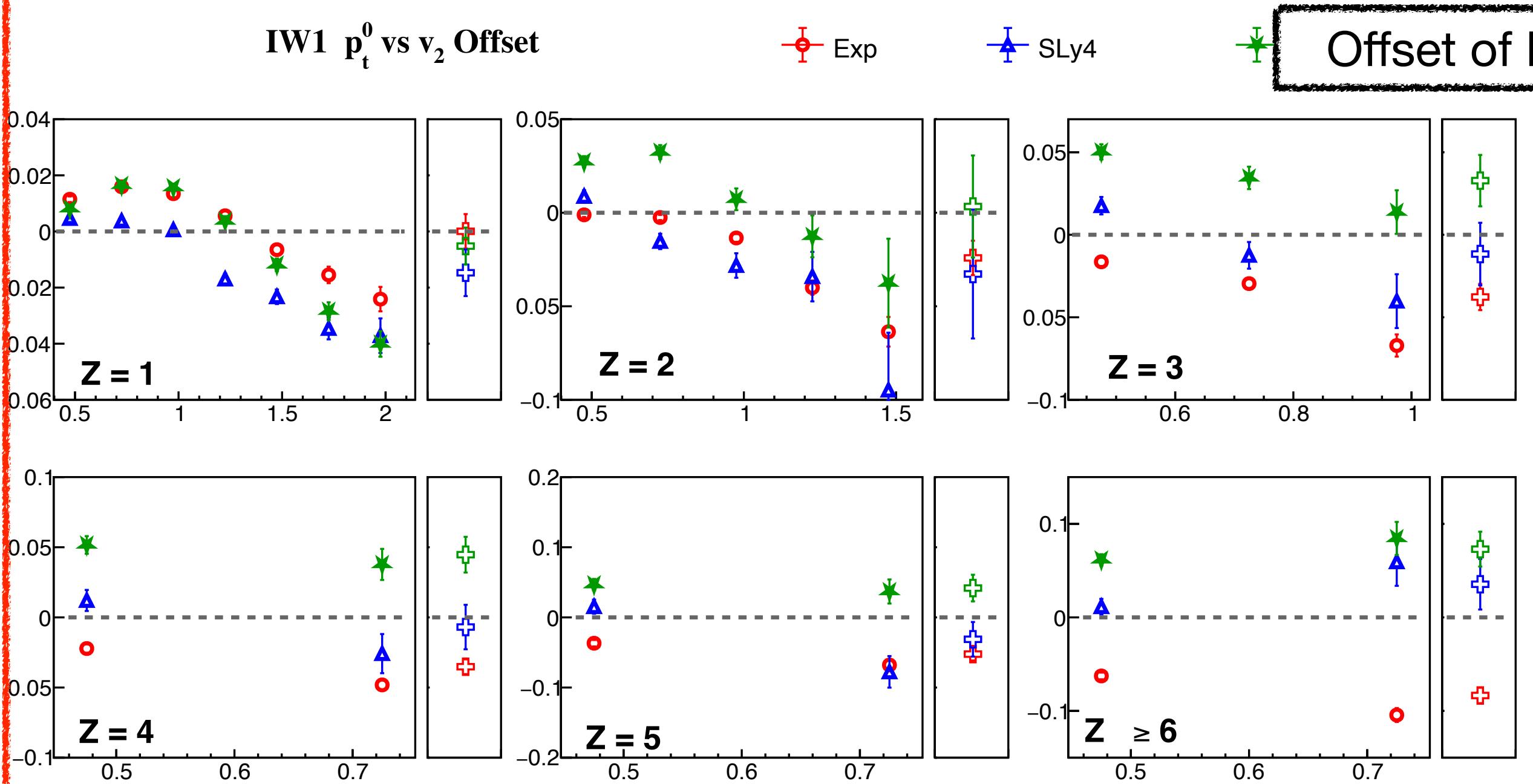
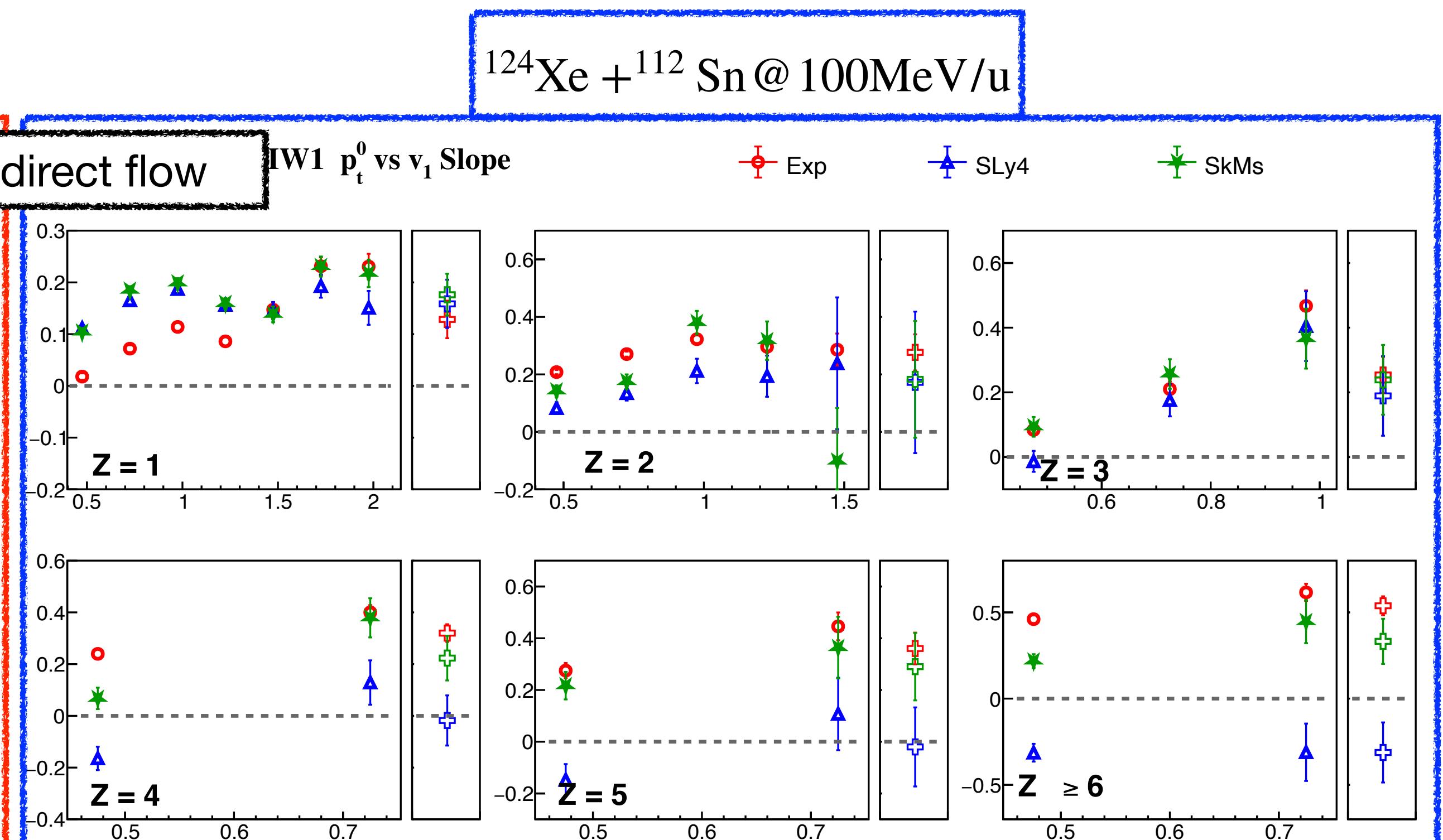
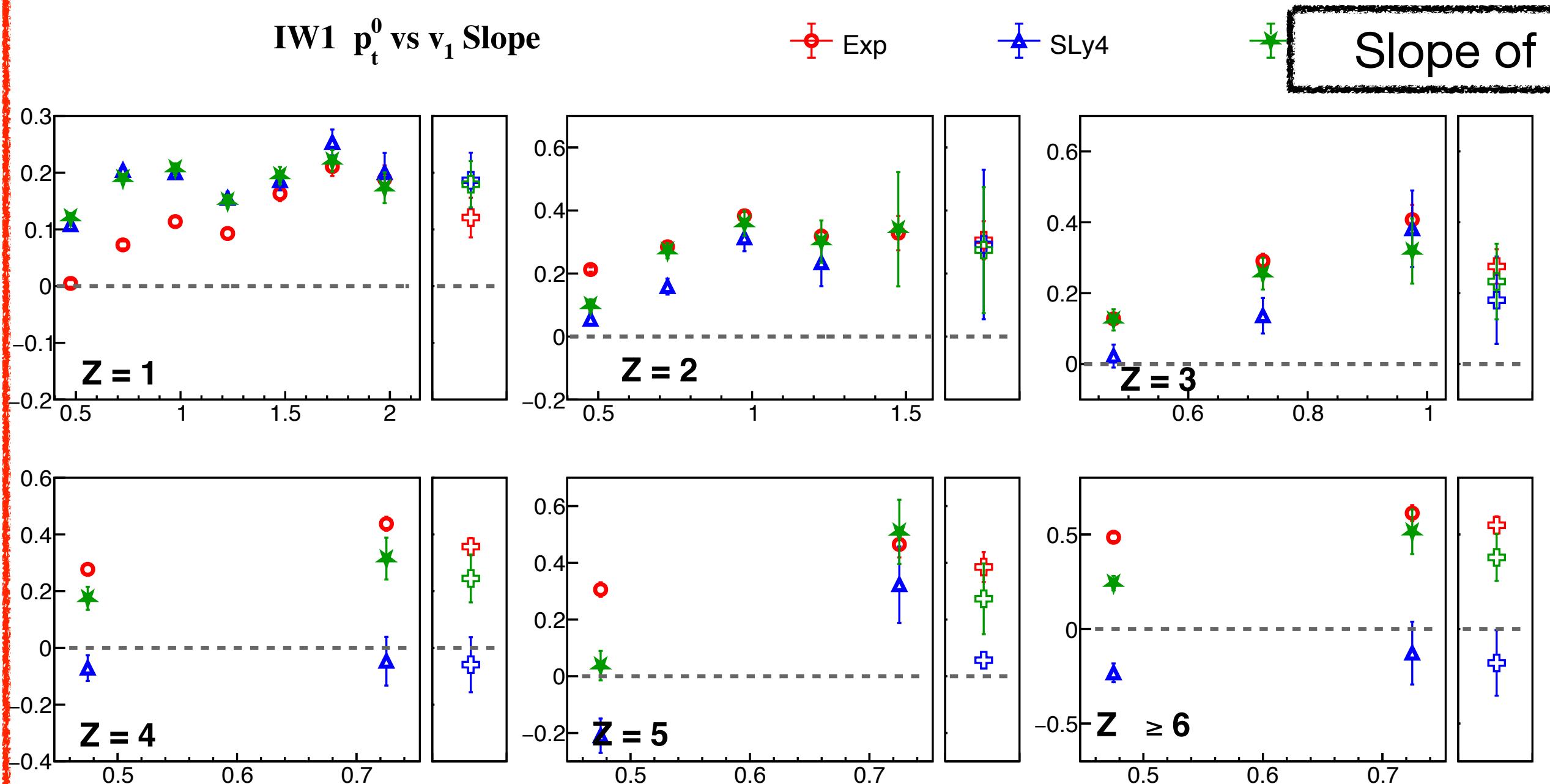
55 MeV/A = $p_t^0 \simeq 1.5$ for Xe + Sn@ 100AMeV55 MeV/A = $p_t^0 \simeq 2.0$ for Ni + Ni@ 52AMeV

TABLE II. The parameters used in the calculations corresponding to $K_0 = 230$ MeV, $m_s^*/m = 0.77$, $S_0 = 32$ MeV, and different values of L and f_I . The parameters α , β , A_{sym} , B_{sym} are in MeV. \tilde{C}_0 and \tilde{D}_0 are fm^3/GeV .

Para.	$(L = 46, f_I = 0.3)$	$(L = 46, f_I = -0.3)$	$(L = 100, f_I = 0.3)$	$(L = 100, f_I = -0.3)$
α			-236.58 (-265.78)	
β			163.95 (194.93)	
γ			1.26 (1.22)	
A_{sym}	83.65 (108.44)	58.57 (62.73)	14.41 (25.32)	-10.67 (-20.40)
B_{sym}	-79.48 (-103.69)	-30.52 (-35.38)	-10.25 (-20.34)	38.72 (47.96)
\tilde{C}_0	-7.92×10^{-4} (-2.08×10^{-3})	0.37 (1.00)	-7.92×10^{-4} (-2.08×10^{-3})	0.37 (1.00)
\tilde{D}_0	0.37 (1.00)	-0.37 (-1.00)	0.37 (1.00)	-0.37 (-1.00)

$^{129}\text{Xe} + ^{124}\text{Sn}$ @ 100MeV/u

Concavity of Direct flow

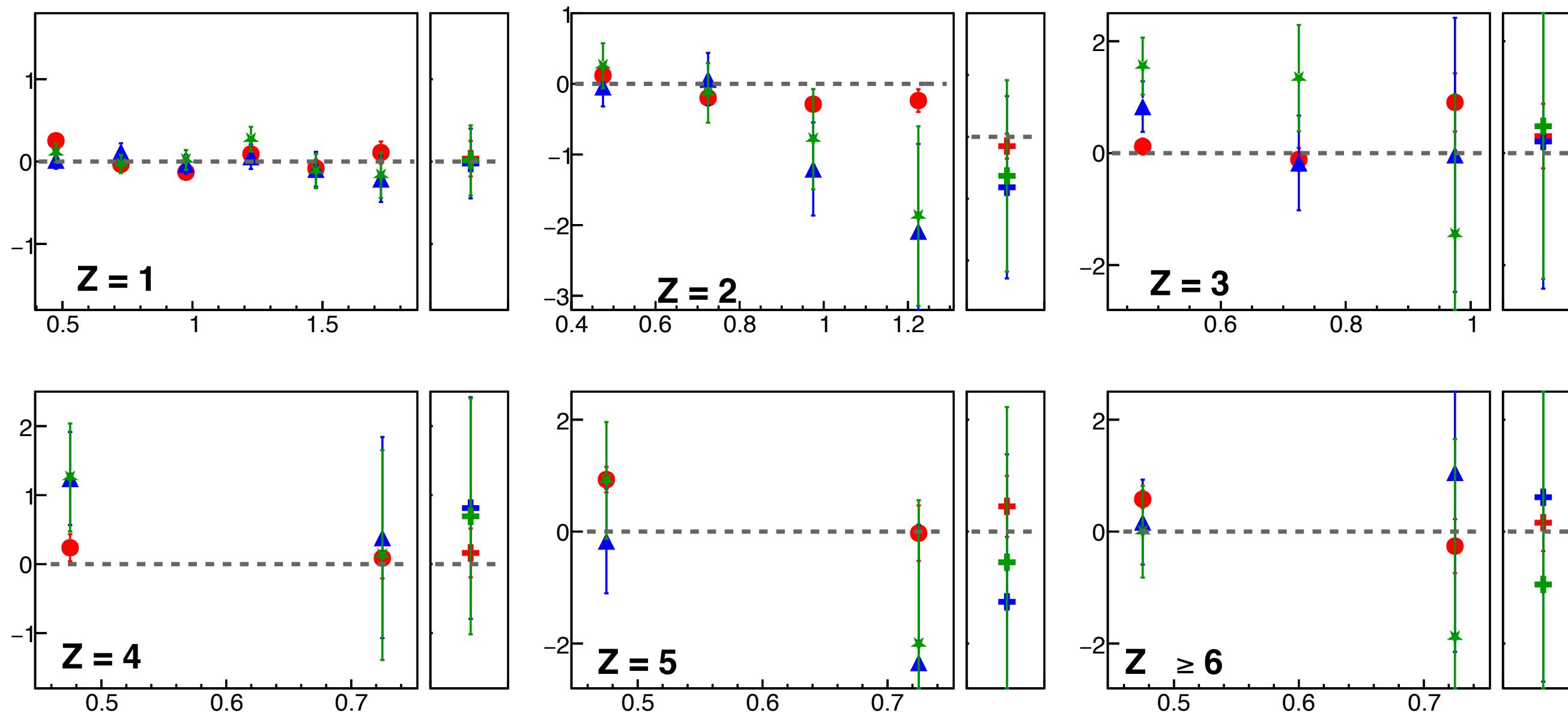
$^{64}\text{Ni} + ^{64}\text{Ni}$ @ 52MeV/u

EW1 p_t^0 vs v_1 Concavity

Exp

SLy4

SkMs



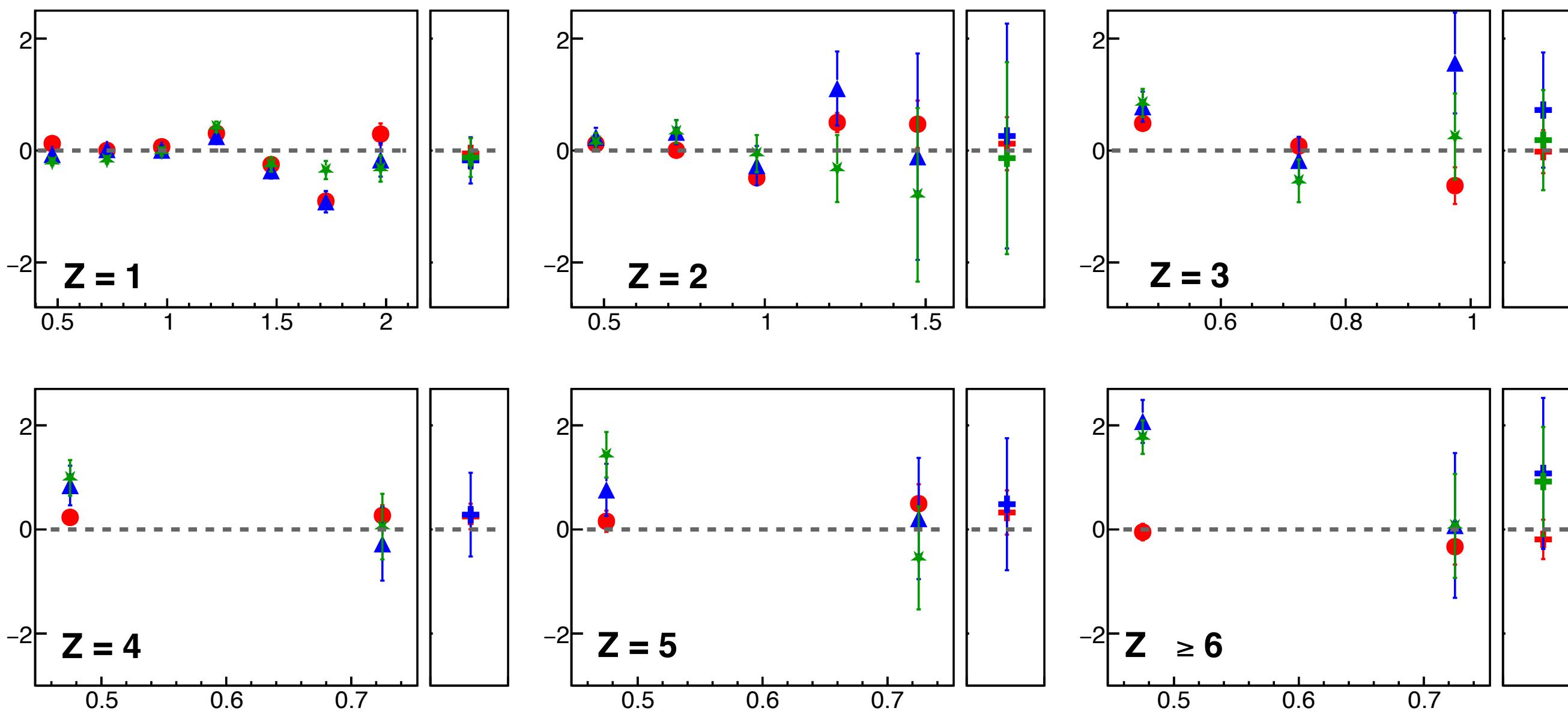
$^{124}\text{Xe} + ^{124}\text{Sn}$ @ 100MeV/u

IW1 p_t^0 vs v_1 Concavity

Exp

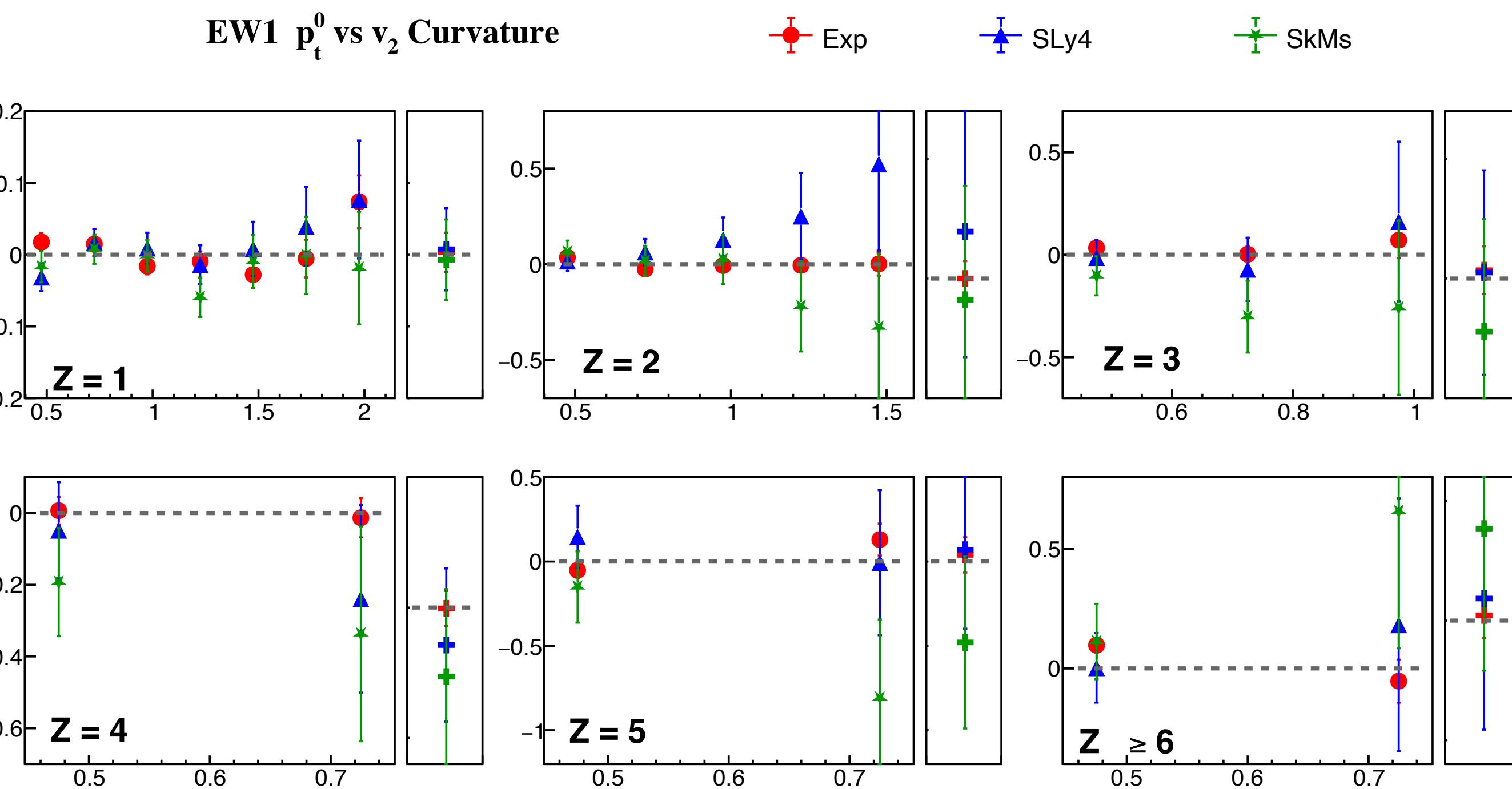
SLy4

SkMs

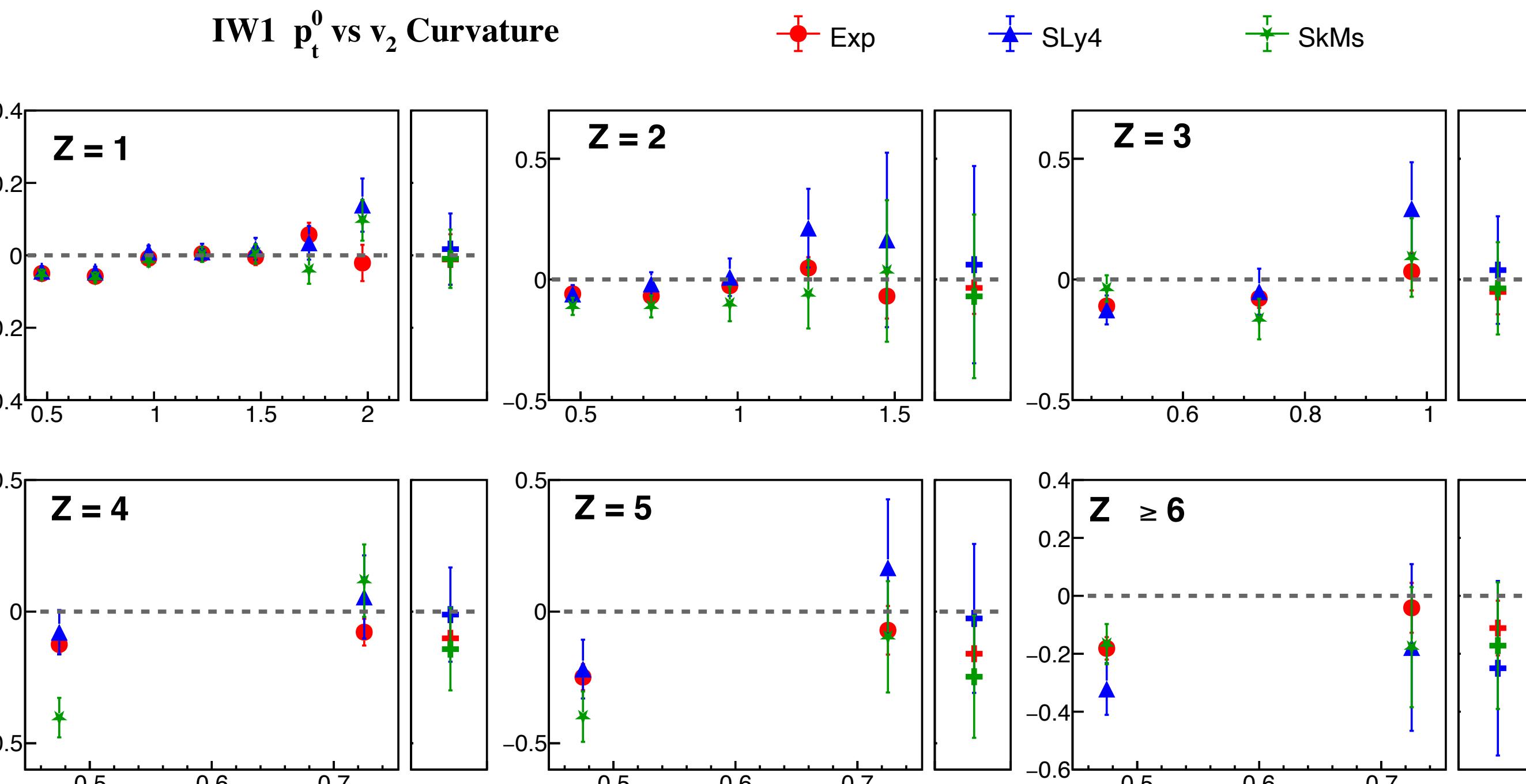


Curvature of Elliptic flow

$^{64}\text{Ni} + ^{64}\text{Ni}$ @ 52MeV/u



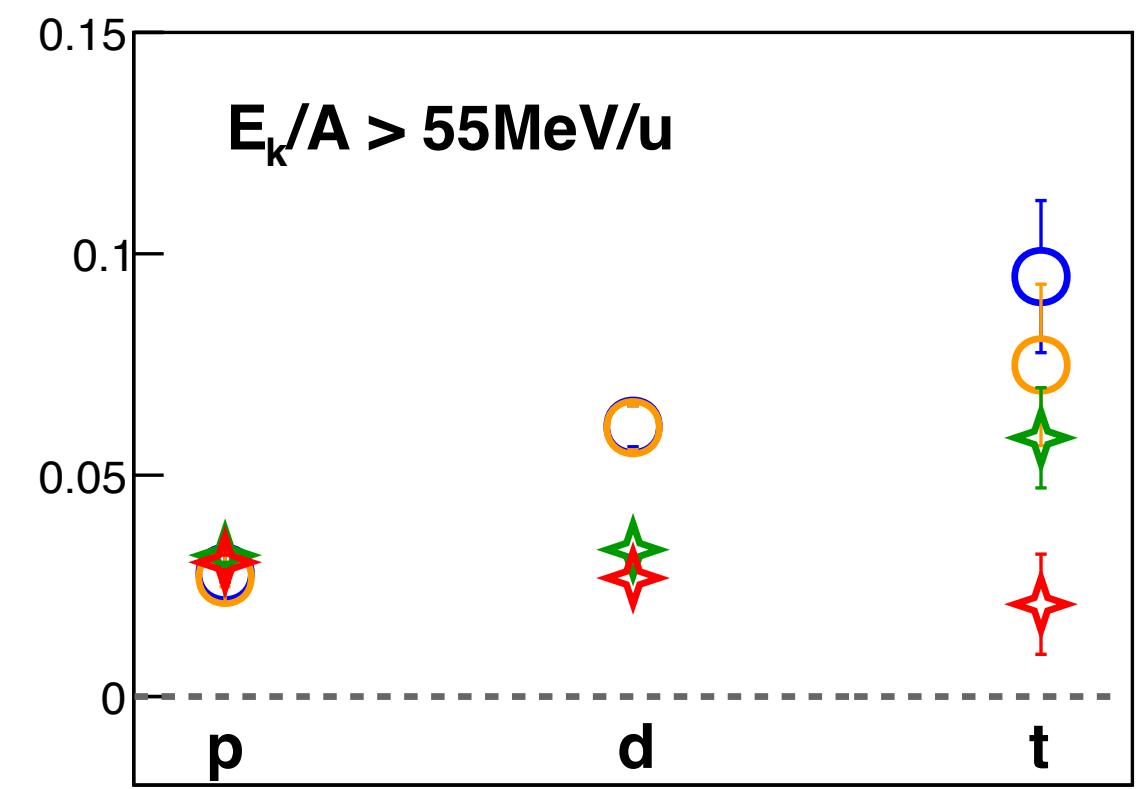
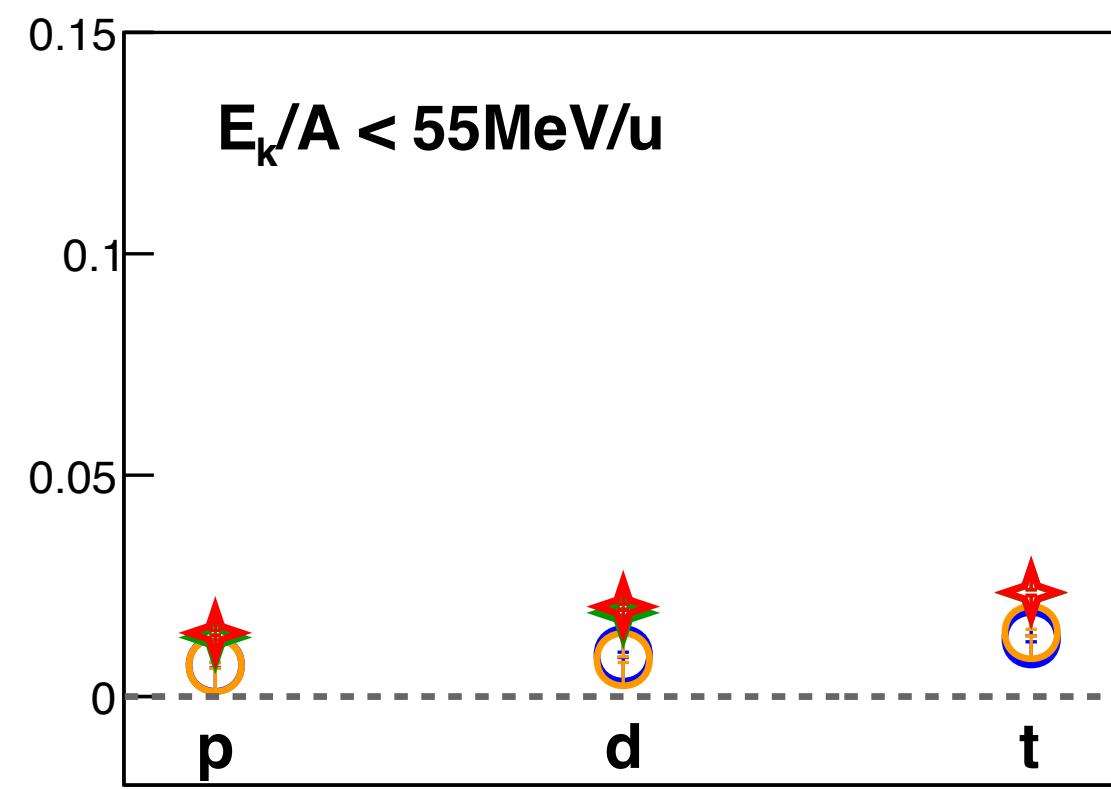
$^{124}\text{Xe} + ^{124}\text{Sn}$ @ 100MeV/u



$^{129,124}\text{Xe} + ^{124}\text{Sn}$ @ 100 & 150MeV/u
Exp, correction factor + system size scaling

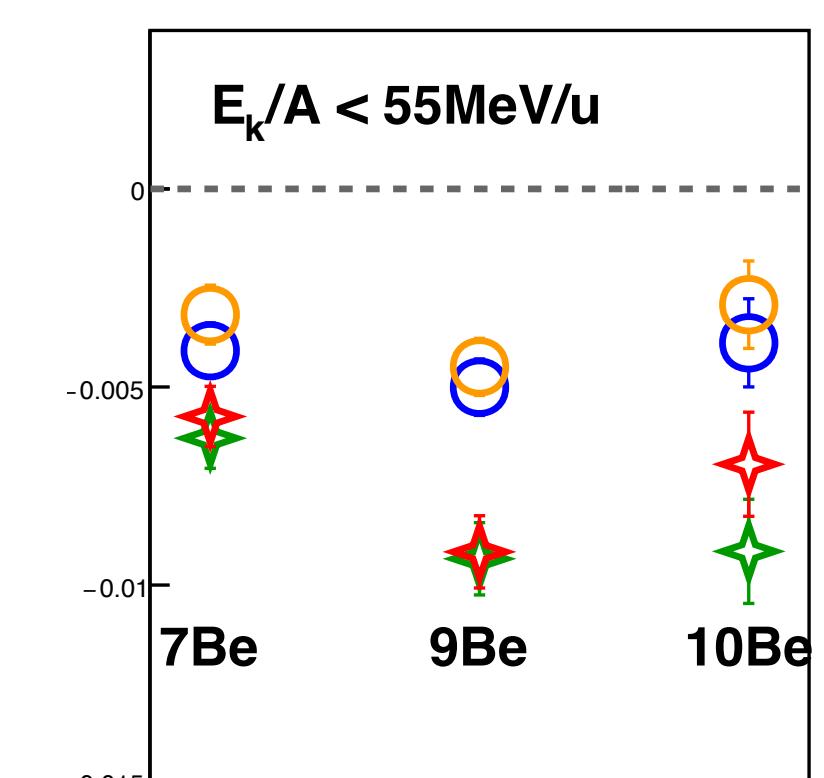
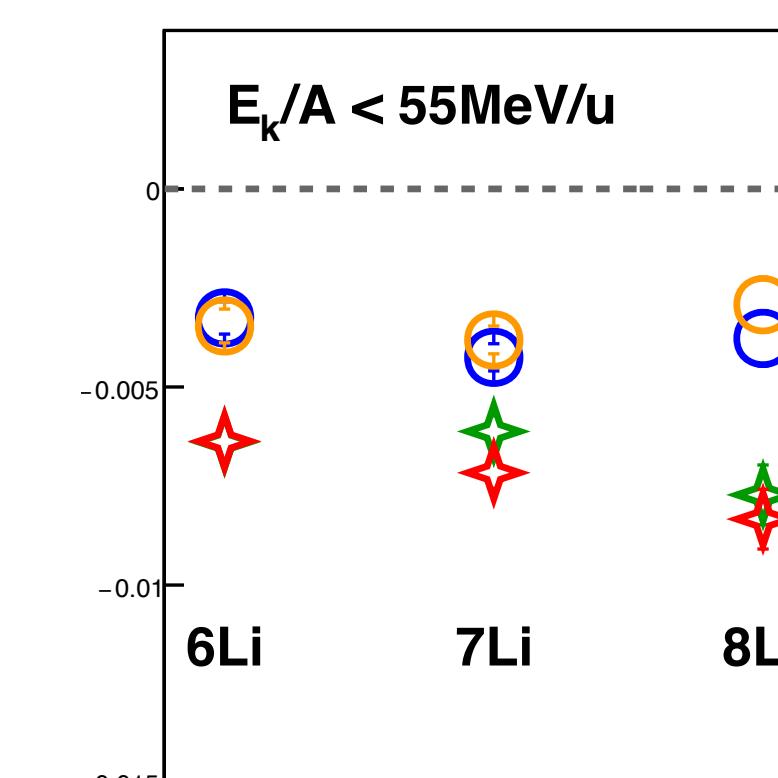
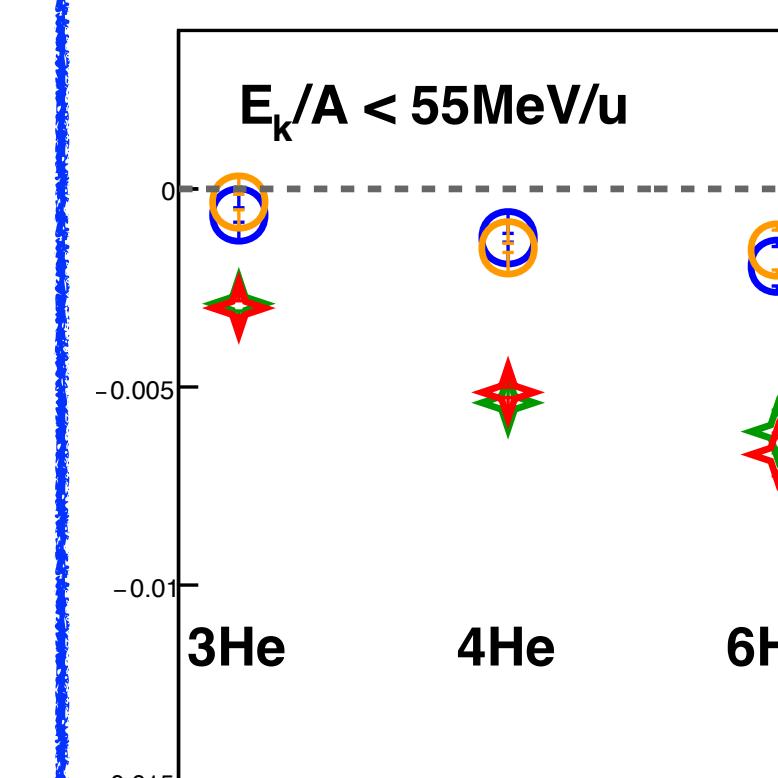
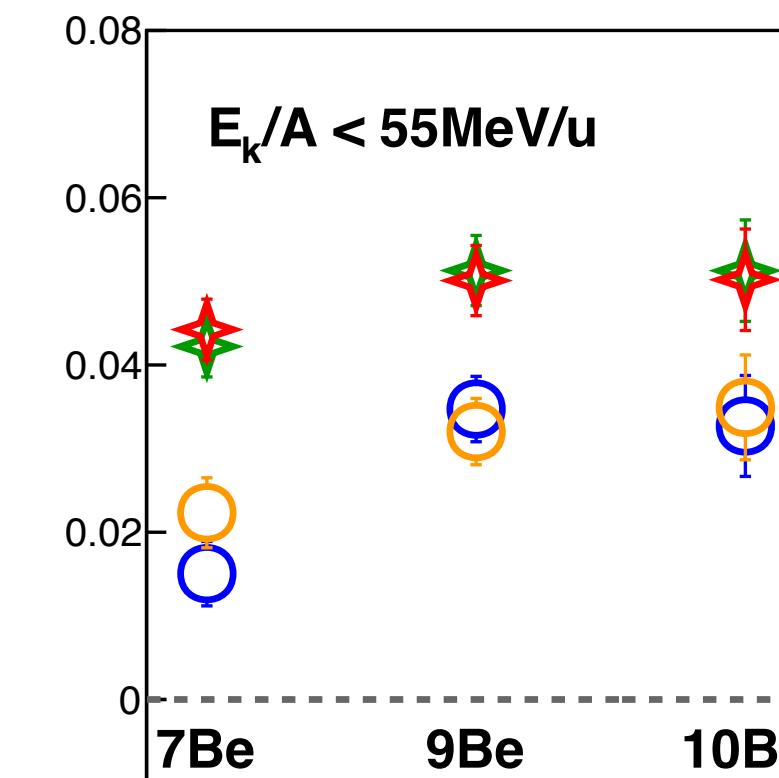
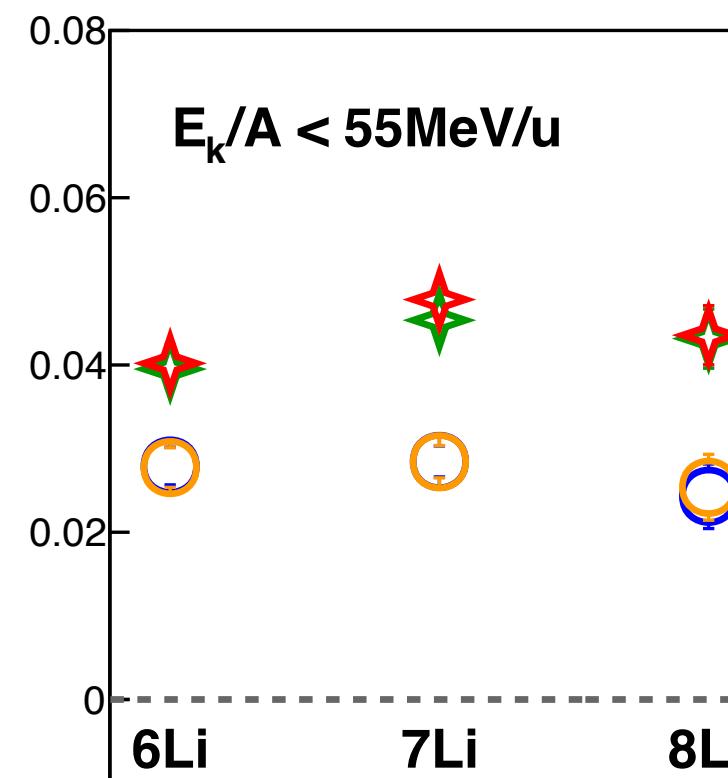
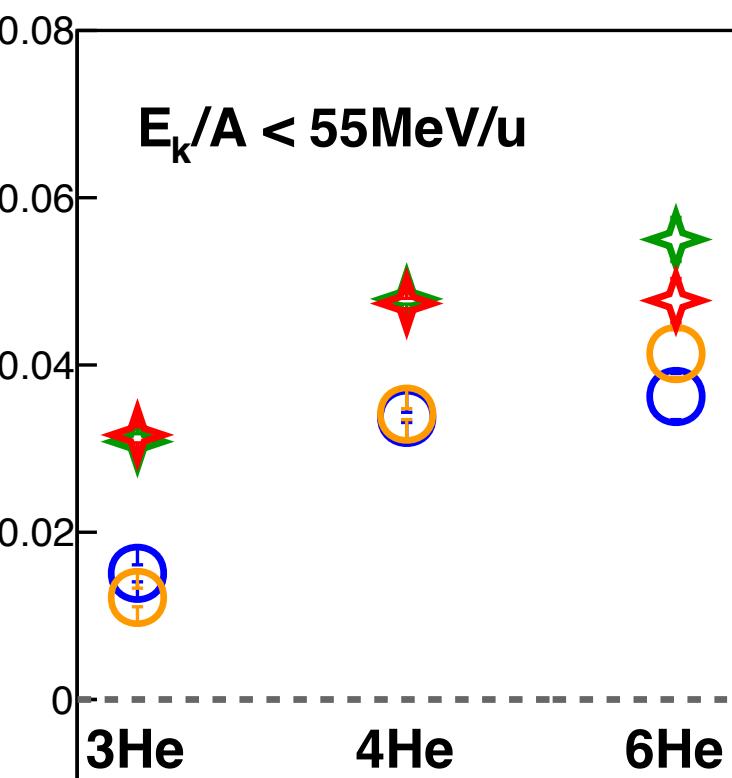
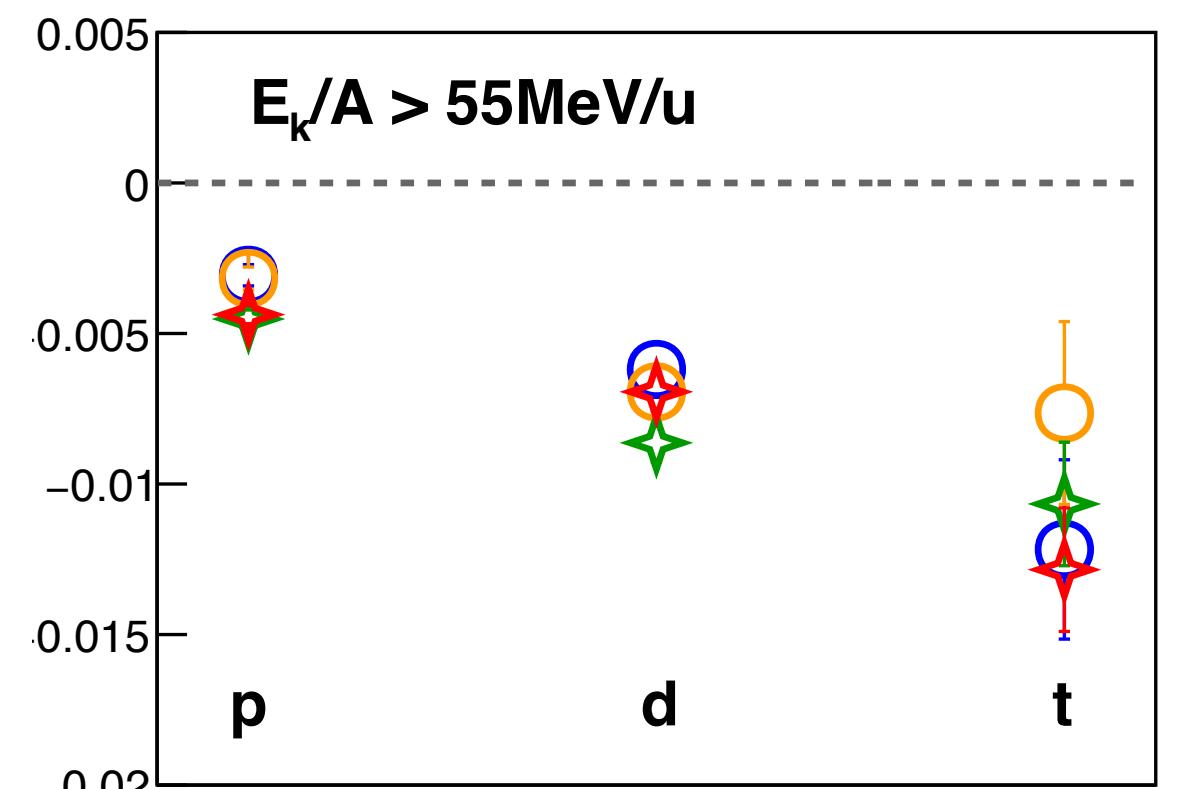
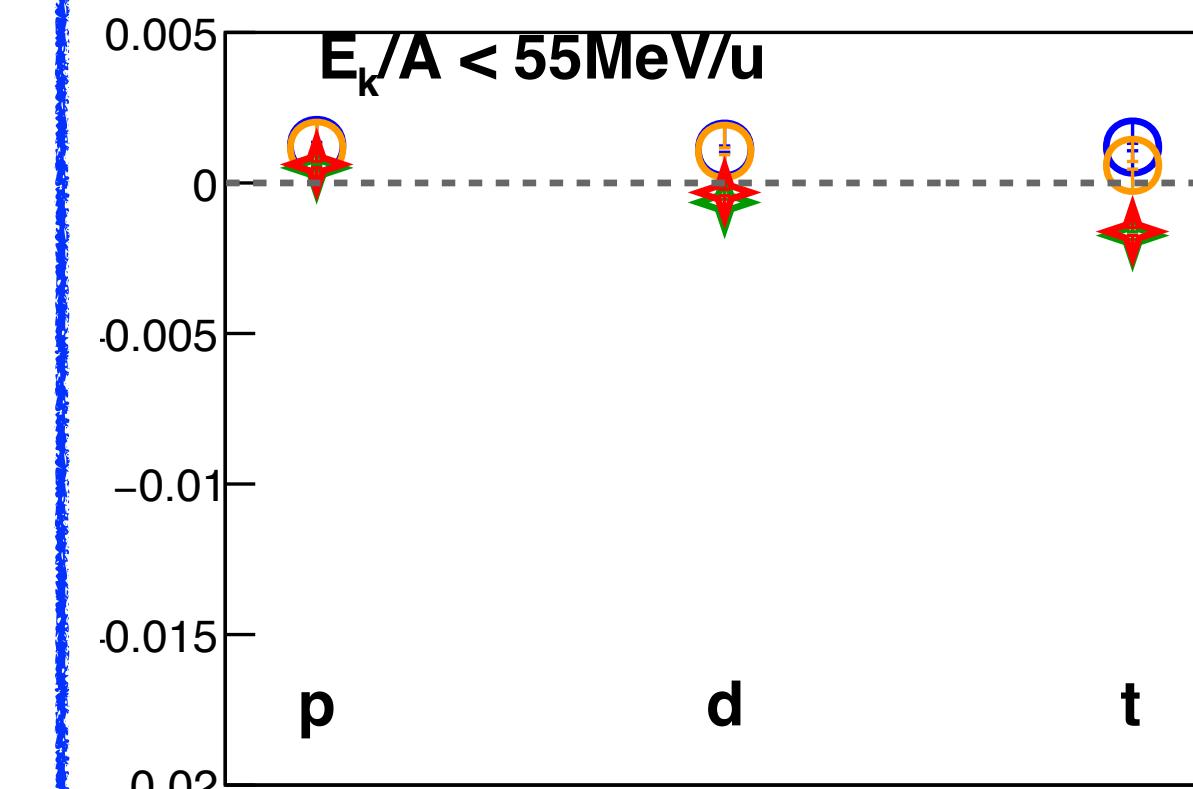
IW1 isotope vs v_1^s Slope

○ 124Xe124Sn 100 ○ 129Xe124Sn 100
★ 124Xe124Sn 150 ★ 129Xe124Sn 150



IW1 isotope vs v_2^s Offset

○ 124Xe124Sn 100 ○ 129Xe124Sn 100
★ 124Xe124Sn 150 ★ 129Xe124Sn 150



$$v_n^s = v_n \langle p_t^0 \rangle / (A_P^{1/3} + A_T^{1/3})$$